

Exercise 1:

1. **Assign type** to the object (extension) denoted by a given expression:
 - a) Charles, Marie, Petr, John
 - b) 1, 2, π
 - c) true, false
 - d) $>$, \geq (binary relations on numbers)
 - e) The successor function on numbers
 - f) Binary functions adding (+), dividing (:)
 - g) $2 + 5$
 - h) $2 + 5 = 7$, $9 > 7$
 - i) The set of prime numbers, the set of even numbers
 - j) The set {Charles, Marie, John}

2. **Assign type** to the object (intension) denoted by a given empirical expression:
 - a) student, rich student, employee, conductor
 - b) to like (somebody), to kick (somebody), look at (something)
 - c) calculate
 - d) Adam calculates $2+5$
 - e) President of (something)
 - f) The salary of (somebody)
 - g) The highest mountain in the world, the President of CR, the richest man in the world
 - h) Miss Universe 2017
 - i) The speed of light, number of planets
 - j) The President of CR is a tennis player

3. **Analyse** the following expressions (apply the *method of analysis*, including *type checking*):
 - a) $2+5=7$
 - b) $\text{Sin}(\pi/2) = 0$
 - c) $\{x \mid \text{Sin}(x)=0\}$ (the set of numbers x such that the sine of $x = 0$)
 - d) Adam is a student.
 - e) Adam calculates $2+5$
 - f) Donald Trump is the president of USA.

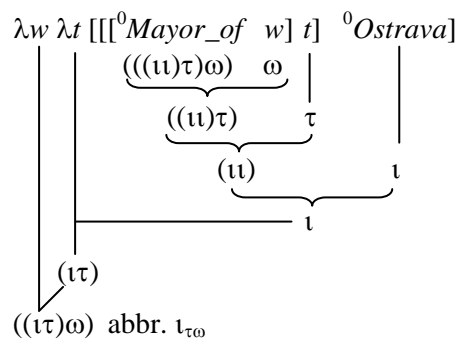
Hint:

Method of analysis consists of these steps:

- a) Assign *types* to objects that receive mention by the analysed expression E
- b) Compose *constructions* of the objects obtained ad a) so that to construct the object denoted by the whole expression E . Semantically simple terms analyse by Trivialization of the denoted object
- c) execute *type checking*, i.e., draw a derivation tree

Example of the analysis of the term „mayor of Ostrava“.

- a) Types: $\text{Mayor_of} / (((\iota)\tau)\omega)$, abbr. $(\iota)_{\tau\omega}$, $\text{Ostrava} / \iota$, $\text{Mayor_of_Ostrava} / \iota_{\tau\omega}$
- b) Synthesis: $\lambda w \lambda t [{}^0 \text{Mayor}_{wt} {}^0 \text{Ostrava}]$
- c) Type checking:



Type checking shortened:

