## **Tutorial 8**

## **Exercise 1**

Let  $C = \{x, y\}$  be a set of clocks such that  $c_x = 2$  and  $c_y = 2$ .

- Draw a picture with all regions for the clocks x and y.
- How many different regions there are on the picture?
- Select four different regions (corner point, line, two areas) and describe them via extended clock constraints (i.e., also diagonal constraints like  $x y \le 1$  etc. can be used).
- Try to find a general formula which describes the number of regions for two clocks and arbitrary maximal constants  $c_x$  and  $c_y$ .

## Exercise 2\*

Draw a region graph of the following timed automaton.

$$x{:=}0{,}y{:=}0 \underbrace{ \begin{pmatrix} 0 < x \leq 1 \\ \ell_0 \end{pmatrix}}_{b \ x=1 \land y=1}^{a} \overset{a}{y{:=}0}$$

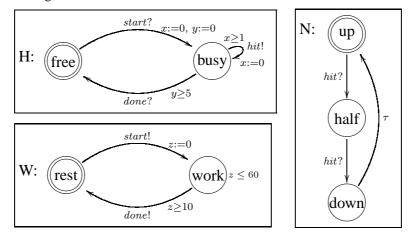
Using the region graph decide whether the following configurations

- $(\ell_0, v)$  where v(x) = 0.7 and v(y) = 0.61
- $(\ell_0, v)$  where v(x) = 0.2 and v(y) = 0.41

are reachable from the initial configuration.

## **Exercise 3**

Consider the following network of timed automata from the lecture.



- Give an example of a timed trace in the network above.
- Which of the following properties are true?
  - A[] (W.rest  $\lor z \le 100$ )
  - $E\langle\rangle$  (W.rest  $\wedge$  H.busy)
  - $A\langle\rangle$  W.rest
  - E[] H.busy
  - W.work -- > W.rest