

# Turingův stroj

# Turingův stroj (TS)

## Cíle prezentace

- seznámit s TS
- předvést simulaci TS
- popsát činnost TS

# Turingův stroj

Turingův stroj si můžeme představit jako model počítače, který se skládá z pásky, řídicí jednotky a hlavy.

# Turingův stroj

Přechodová funkce

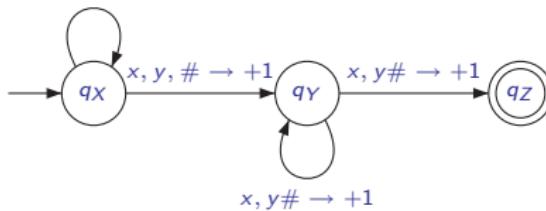
$$\delta(q_X, x) = (q_X, x, +1)$$

$$\delta(q_Y, y) = (q_Y, y, +1)$$

$$\delta(q_Z, \#) = (q_Z, \#, 0)$$



graf TS



- Páska je rozdělena na jednotlivá pole. V těchto polích jsou obsaženy symboly, které se dají číst a rovněž přepisovat.

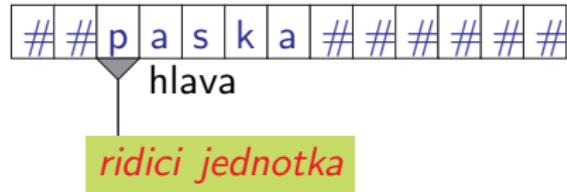
# Turingův stroj

Přechodová funkce

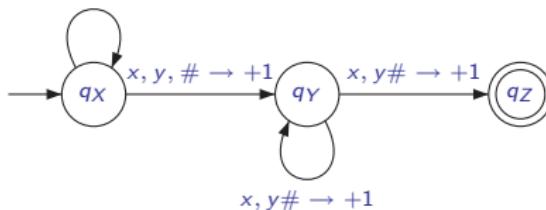
$$\delta(q_X, x) = (q_X, x, +1)$$

$$\delta(q_Y, y) = (q_Y, y, +1)$$

$$\delta(q_Z, \#) = (q_Z, \#, 0)$$



graf TS



- V řídicí jednotce se udržuje aktuální stav TS. Řídicí jednotka vyhodnocuje symboly na pásmu a podle přechodové funkce může měnit symboly na pásmu a posouvat hlavu.

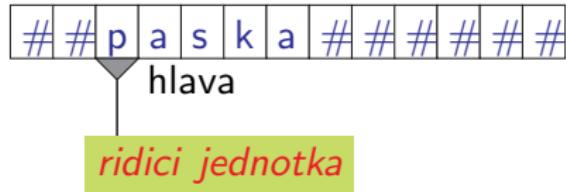
# Turingův stroj

Přechodová funkce

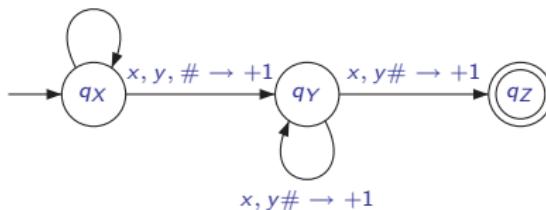
$$\delta(q_X, x) = (q_X, x, +1)$$

$$\delta(q_Y, y) = (q_Y, y, +1)$$

$$\delta(q_Z, \#) = (q_Z, \#, 0)$$



graf TS



- Hlava slouží pro čtení a zápis symbolů na pásku. Posouvá se po pásku podle pokynů řídicí jednotky.

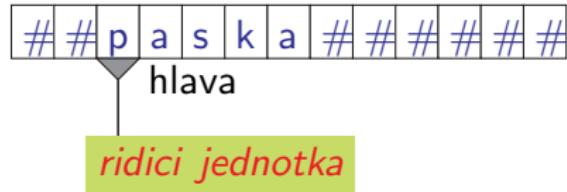
# Turingův stroj

Přechodová funkce

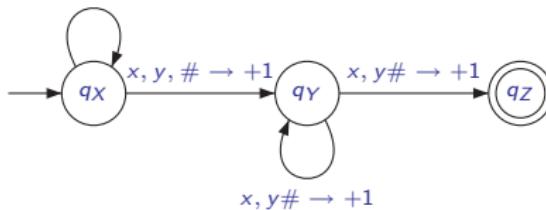
$$\delta(q_X, x) = (q_X, x, +1)$$

$$\delta(q_Y, y) = (q_Y, y, +1)$$

$$\delta(q_Z, \#) = (q_Z, \#, 0)$$



graf TS



- Graf TS slouží pro zobrazení simulace.

## Turingův stroj

Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) \equiv (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A = 1)$$

$$\delta(g_1, B) = (g_1, B - 1)$$

$$\delta(q_1, A) = (q_1, A + 1)$$

$$\delta(g, B) = (g, B + 1)$$

$$\delta(g_i, \#) = (g_i, \Delta - 1)$$

$$\delta(g, A) = (g, A + 1)$$

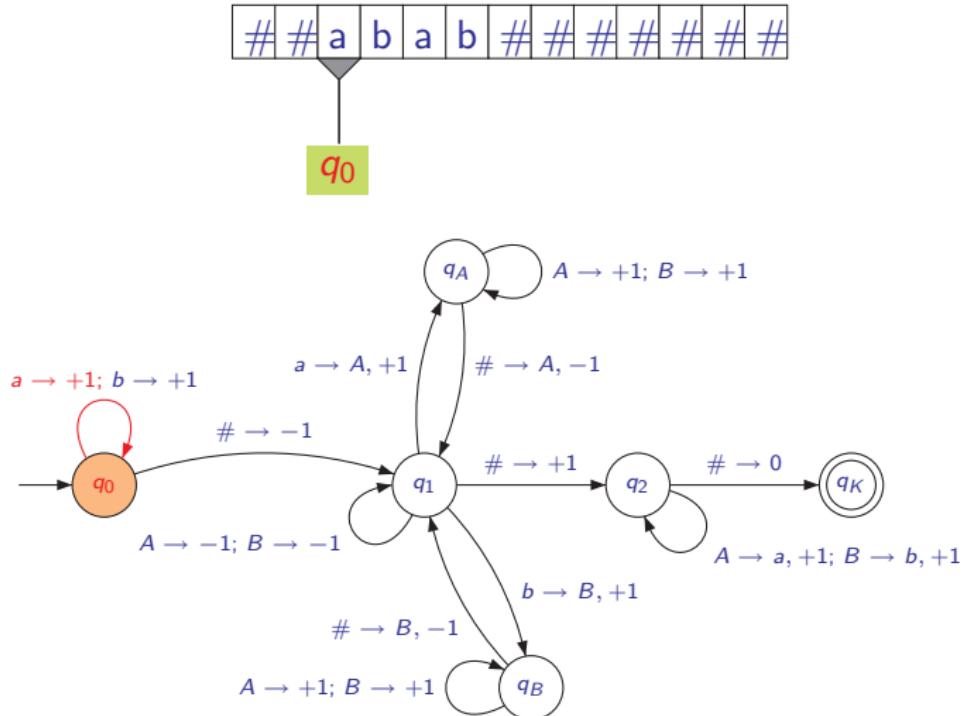
$$\delta(\tilde{\pi}, B) = (\tilde{\pi}, B + 1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$



Popis

- Nejprve TS nalezne konec slova.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

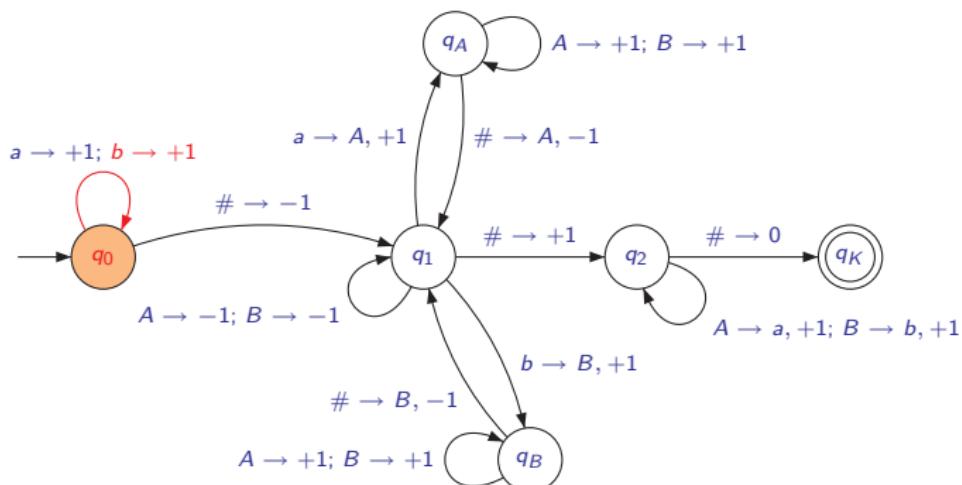
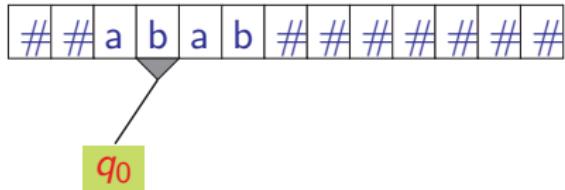
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- Nejprve TS nalezne konec slova.

## Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) \equiv (q_B, A, +1)$$

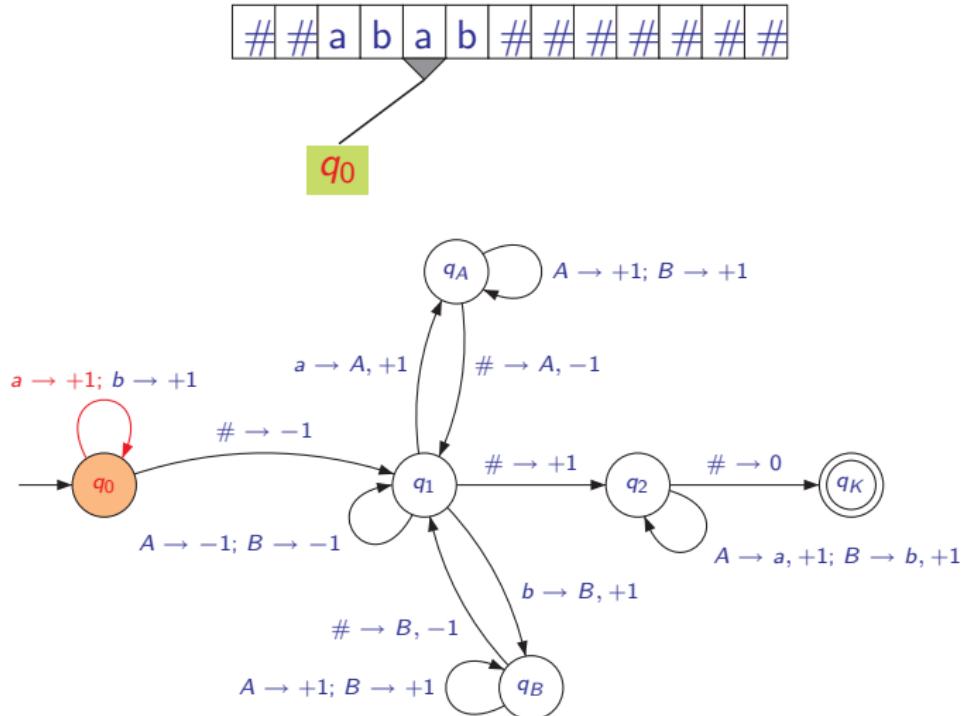
$$\delta(q_B, B) \equiv (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(g_3, A) = (g_3, a+1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



Popis

- Nejprve TS nalezne konec slova.

## Turingův stroj

Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) \equiv (q_B, A, +1)$$

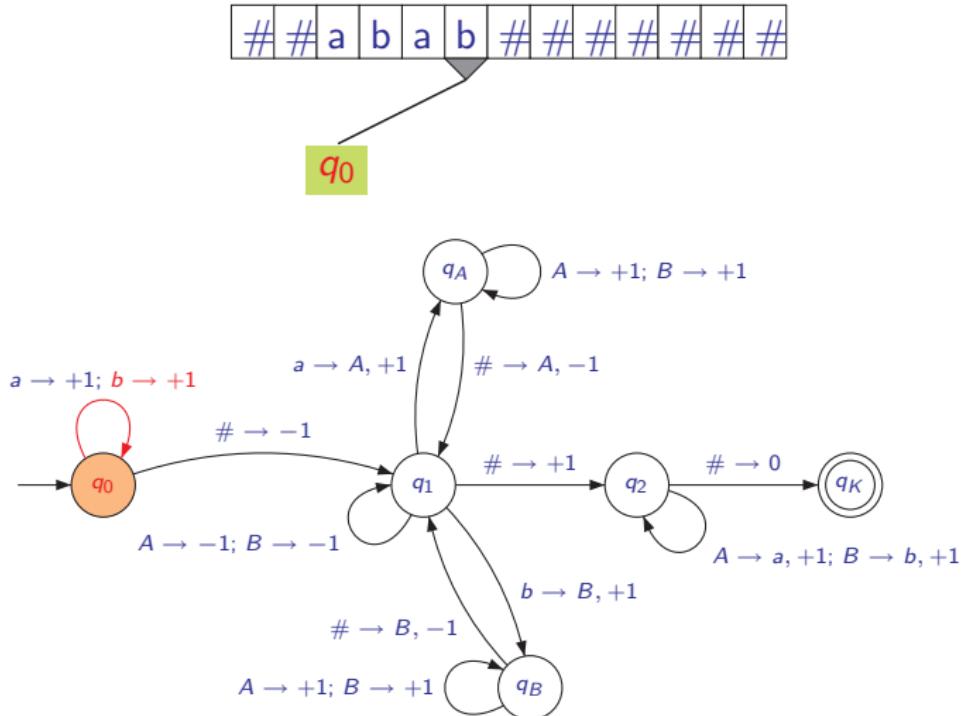
$$\delta(q_B, B) \equiv (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(g_3, A) = (g_3, a+1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



Popis

- Nejprve TS nalezne konec slova.

## Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) \equiv (q_1, B, -1)$$

$$\delta(q_A, A) \equiv (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

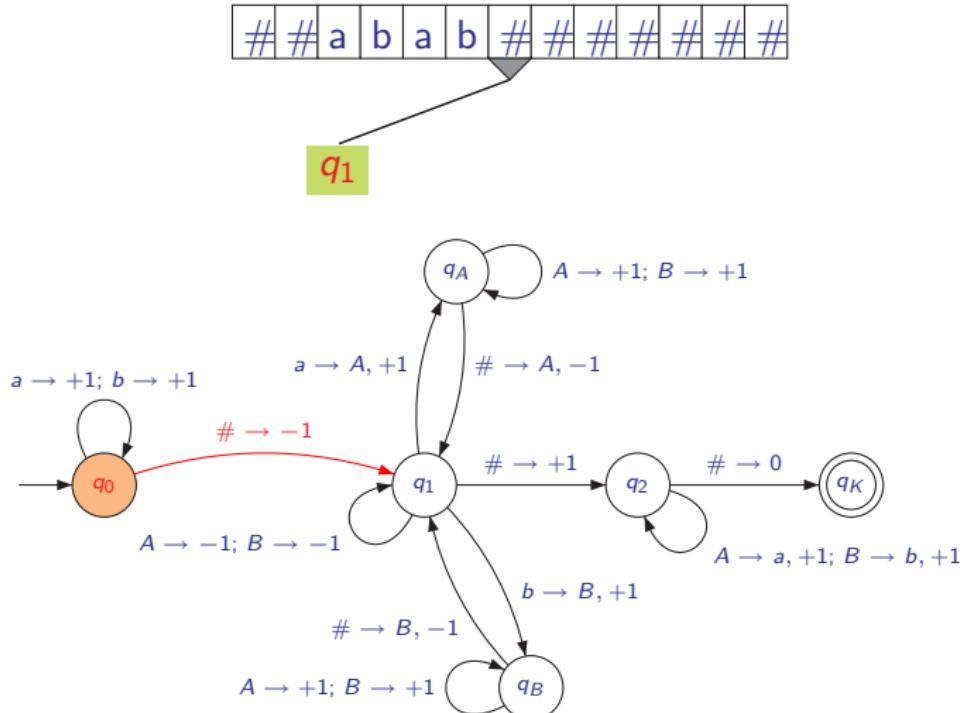
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(g_2, A) = (g_2 - 3 + 1)$$

$$\delta(q_2, B) = (q_2, b + 1)$$

$$\delta(q_2 \#) = (q_K \# 0)$$



Popis

- Nyní přejde do stavu  $q_1$ :

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

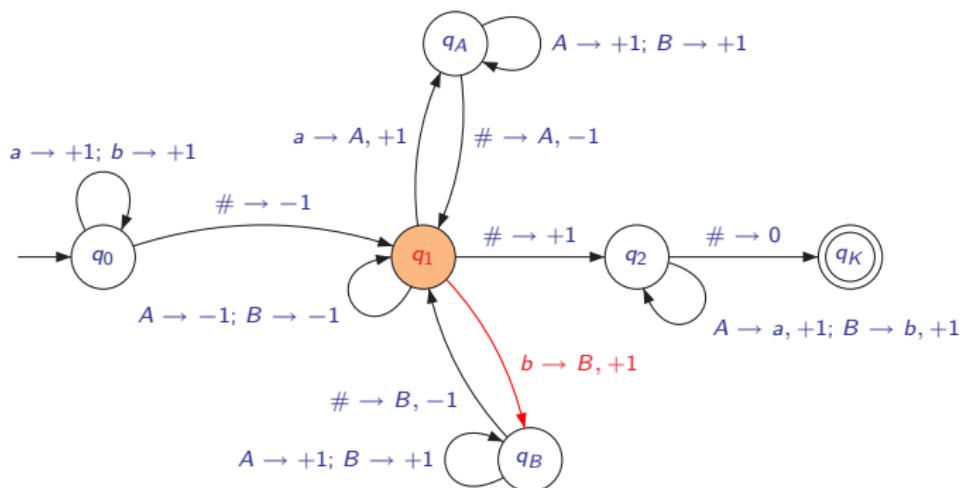
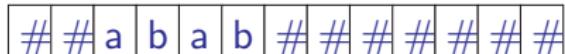
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá symboly **abab**, které následně označí.

## Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) \equiv (q_1, B, -1)$$

$$\delta(q_A, A) \equiv (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A + 1)$$

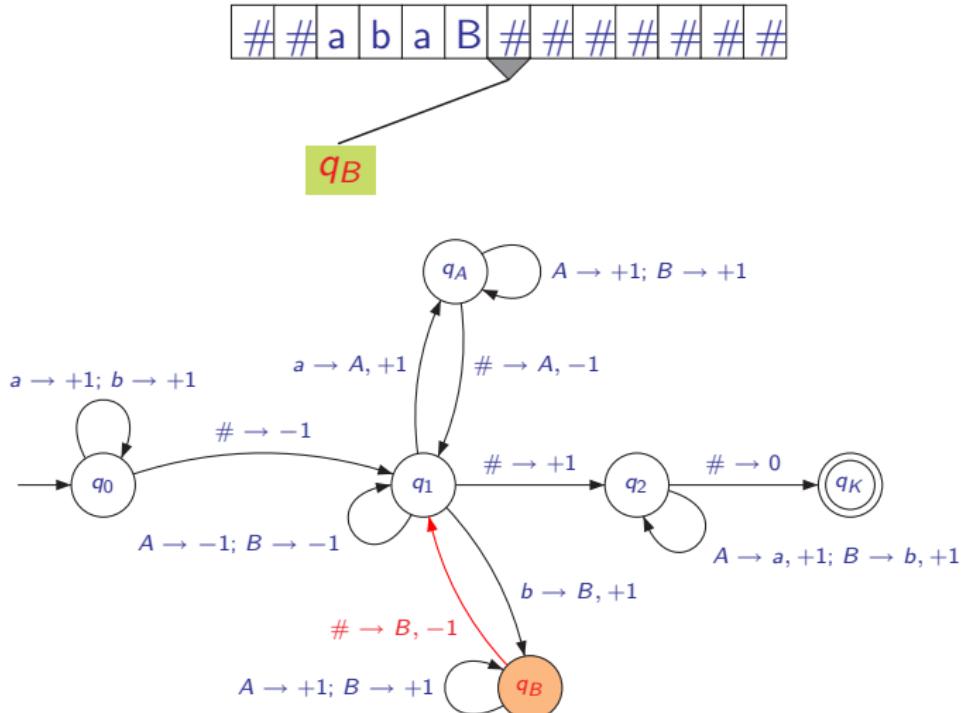
$$\delta(g_B, B) \equiv (g_B, B + 1)$$

$$\delta(g_B, \#) = (g_1, B=1)$$

$$\delta(g_2, A) = (g_2 - 3 + 1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$



Popis

- TS hledá první volnou pozici, na kterou uloží symbol B.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

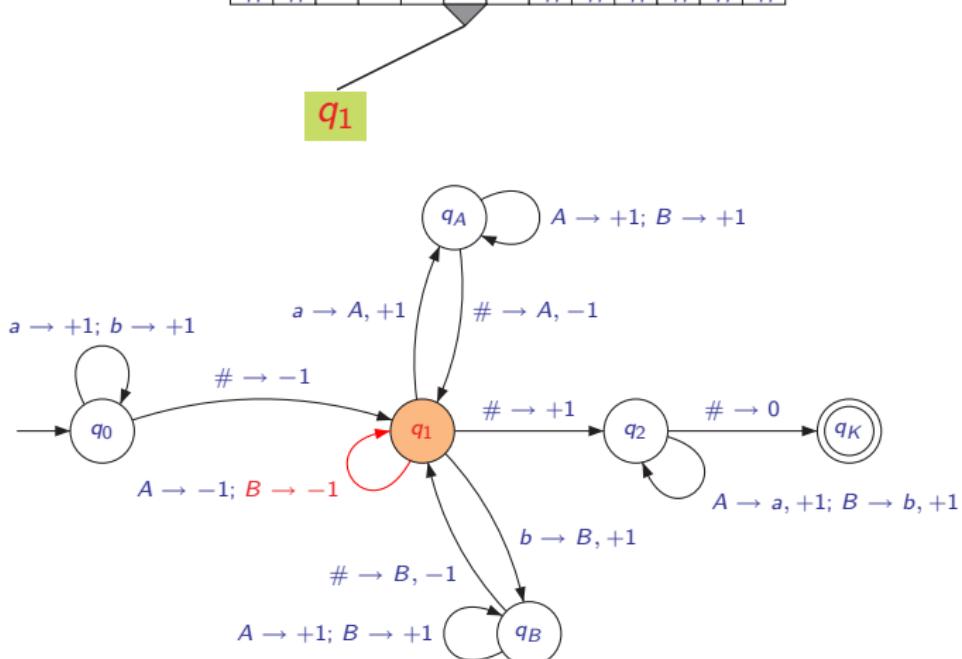
$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$

#	#	a	b	a	B	B	#	#	#	#	#	#	#
---	---	---	---	---	---	---	---	---	---	---	---	---	---



## Popis

- TS hledá symboly **abab**, které následně označí.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

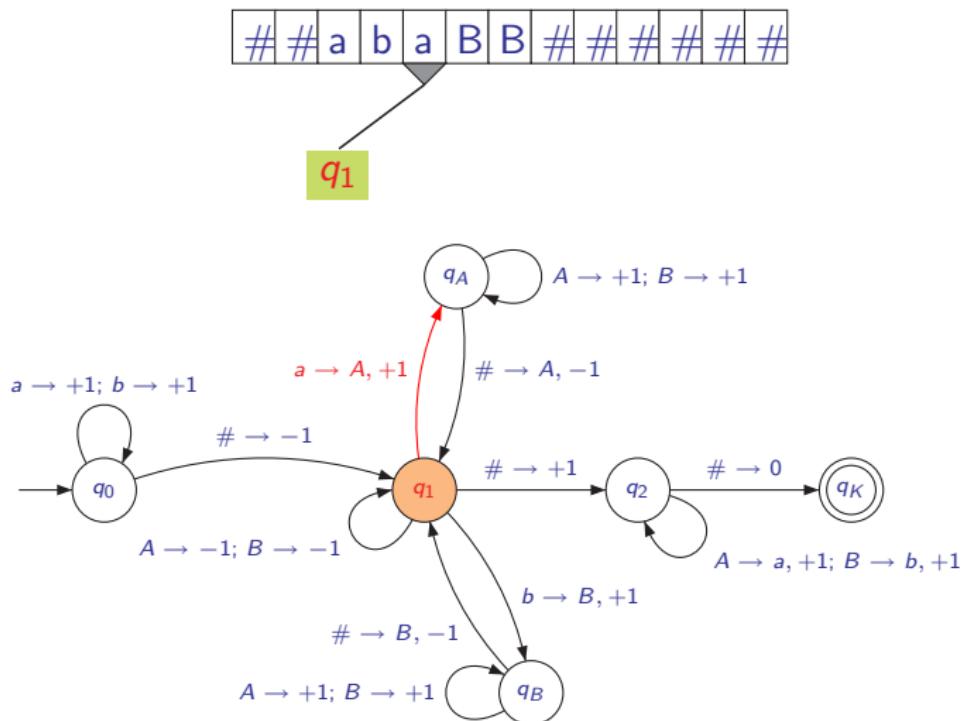
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá symboly **abab**, které následně označí.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

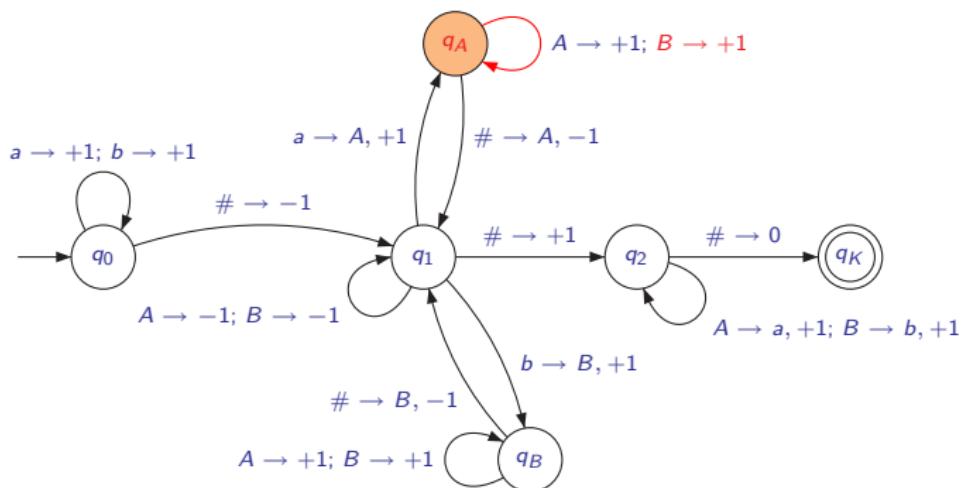
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá první volnou pozici, na kterou uloží symbol A.

## Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) \equiv (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(g_A, B) = (g_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A + 1)$$

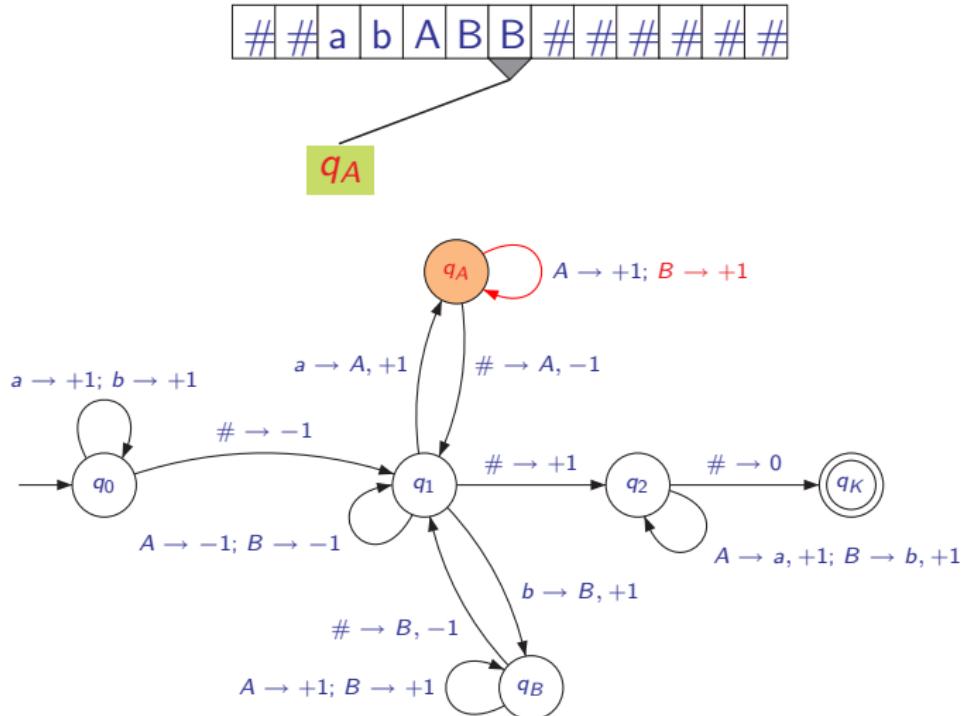
$$\delta(q_B, B) = (q_B, B + 1)$$

$$\delta(q_B, \#) = (q_1, B - 1)$$

$$\delta(q_3, A) = (q_3 - 3 + 1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, \#) = (q_1, \#, 0)$$



Popis

- TS hledá první volnou pozici, na kterou uloží symbol A.

## Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) \equiv (q_1, B, -1)$$

$$\delta(q_A, A) \equiv (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A + 1)$$

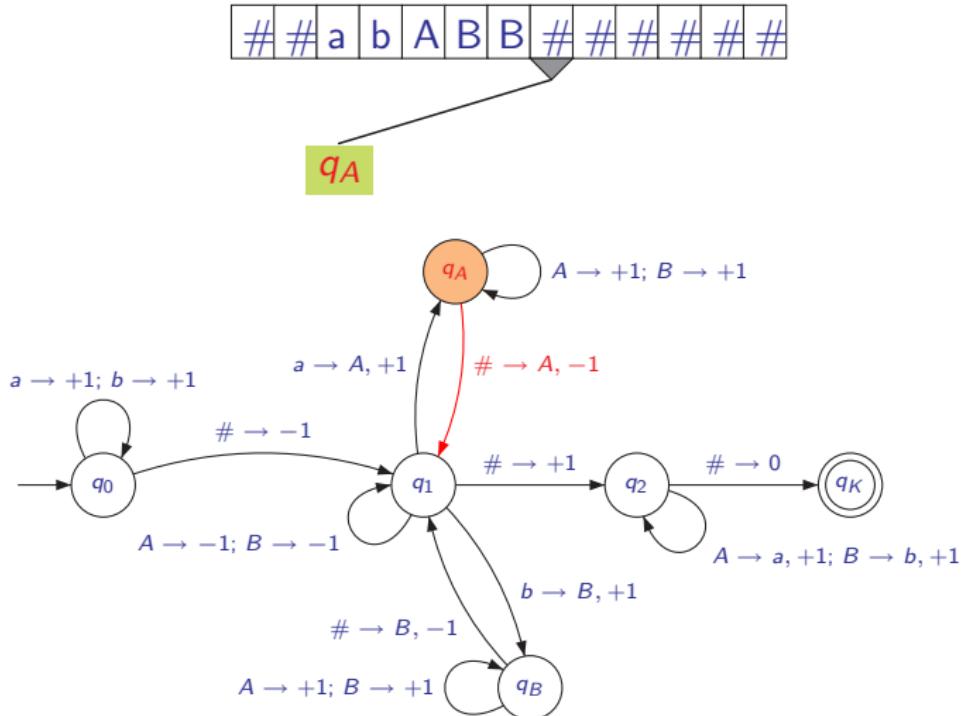
$$\delta(g_B, B) \equiv (g_B, B + 1)$$

$$\delta(q_B, \#) = (q_1, B=1)$$

$$\delta(g_3, A) = (g_3 - 3 + 1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, \#) = (q_1, \#, 0)$$



Popis

- TS hledá první volnou pozici, na kterou uloží symbol A.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

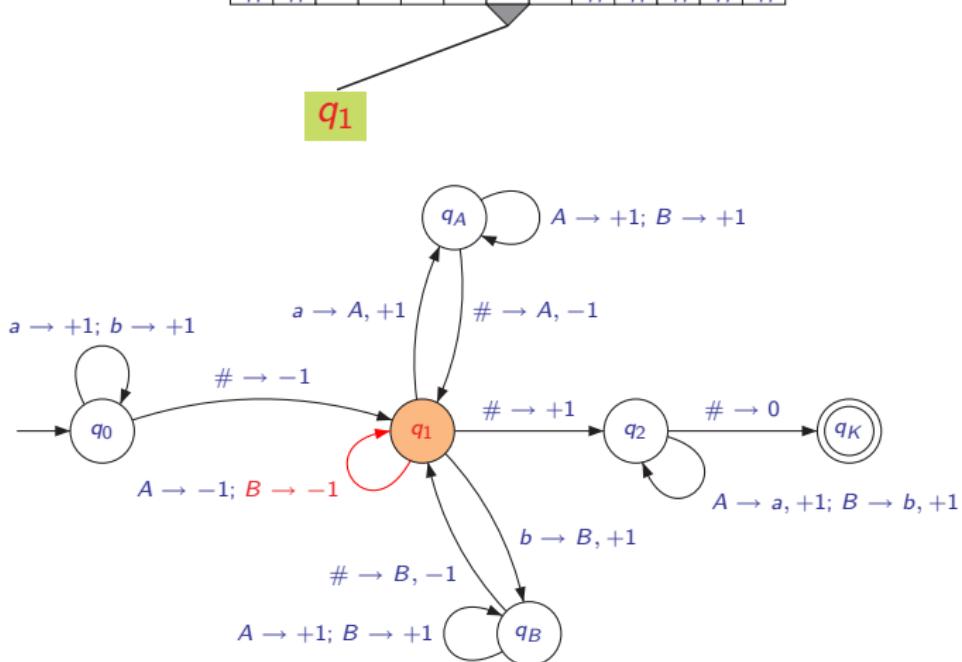
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá symboly **abab**, které následně označí.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

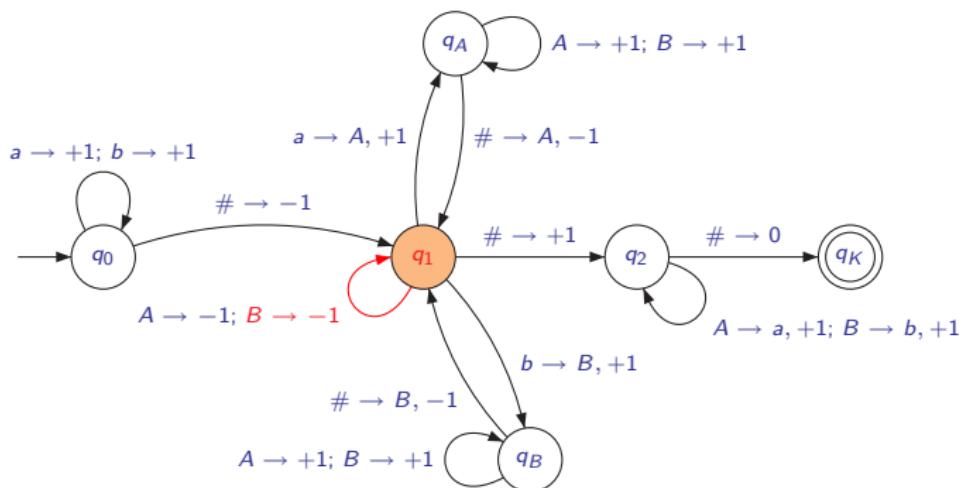
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá symboly abab, které následně označí.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

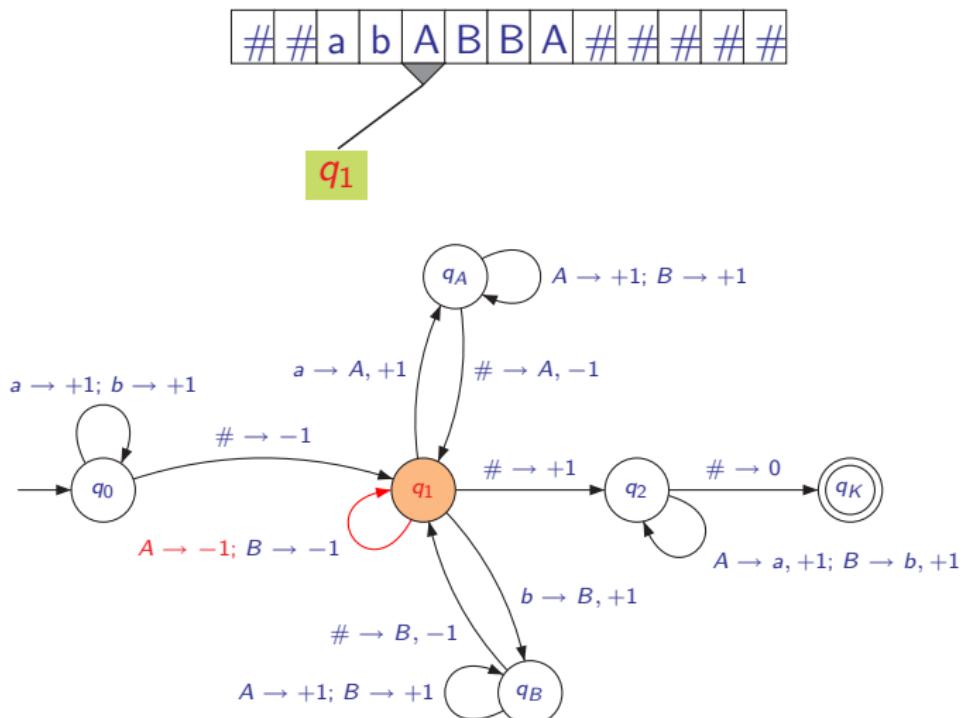
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá symboly **abab**, které následně označí.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

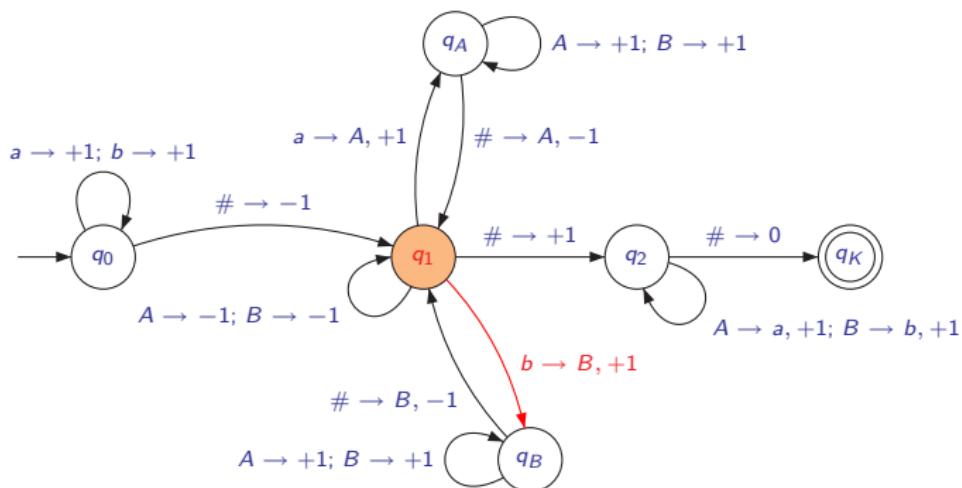
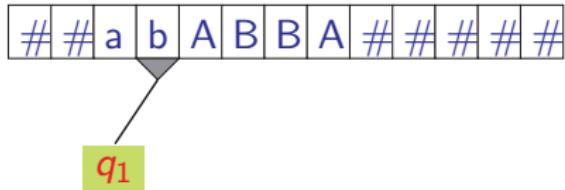
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá symboly **abab**, které následně označí.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

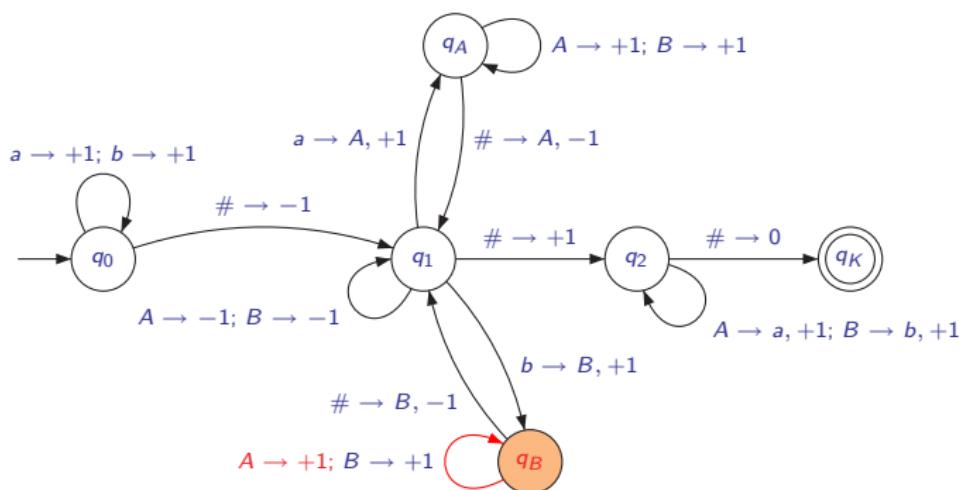
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá první volnou pozici, na kterou uloží symbol B.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

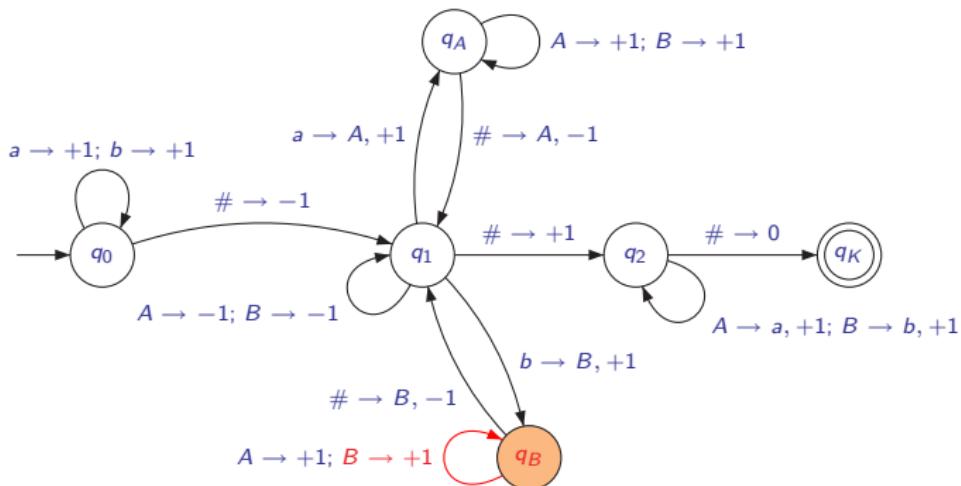
$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



$q_B$



## Popis

- TS hledá první volnou pozici, na kterou uloží symbol B.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

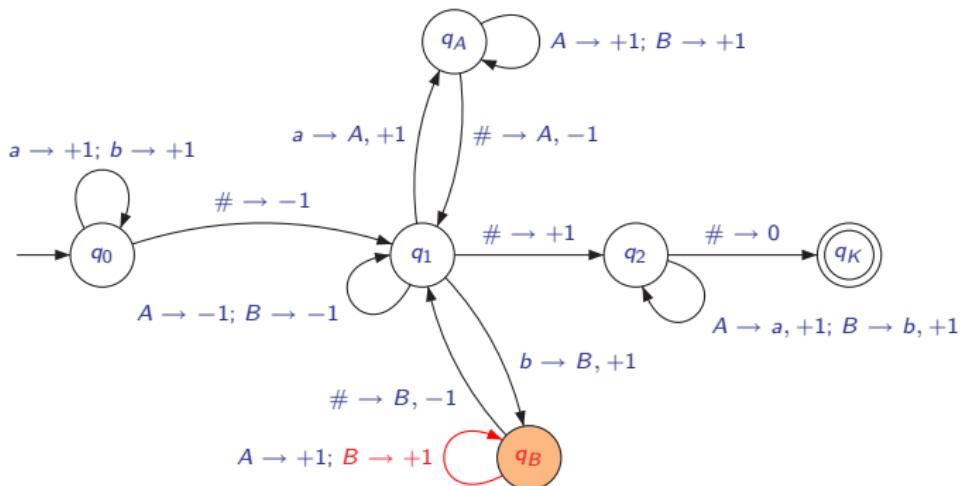
$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



$q_B$



## Popis

- TS hledá první volnou pozici, na kterou uloží symbol B.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

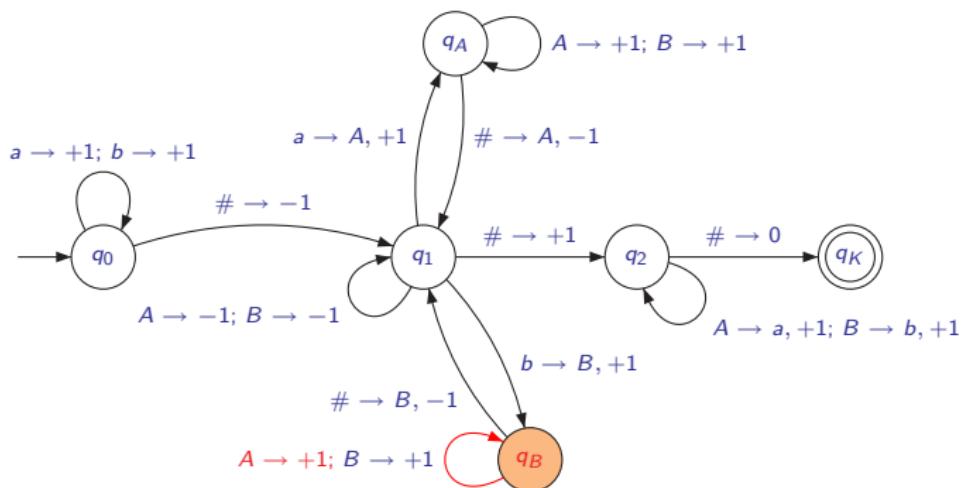
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá první volnou pozici, na kterou uloží symbol B.

## Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) \equiv (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A = 1)$$

$$\delta(g_1, B) = (g_1, B - 1)$$

$$\delta(q_1, A) = (q_1, A + 1)$$

$$\delta(g, B) = (g, B + 1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(g_A, \#) = (g_1, A, -1)$$

$$\delta(\tilde{\pi}, B) = (\tilde{\pi}, B + 1)$$

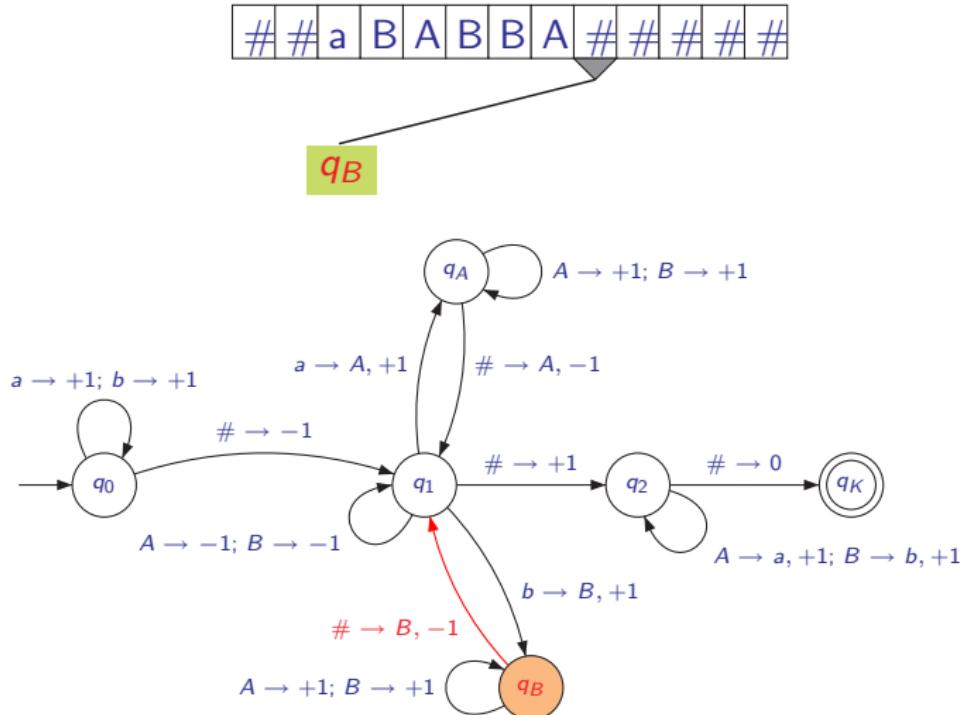
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



Popis

- TS hledá první volnou pozici, na kterou uloží symbol B.

## Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) \equiv (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A + 1)$$

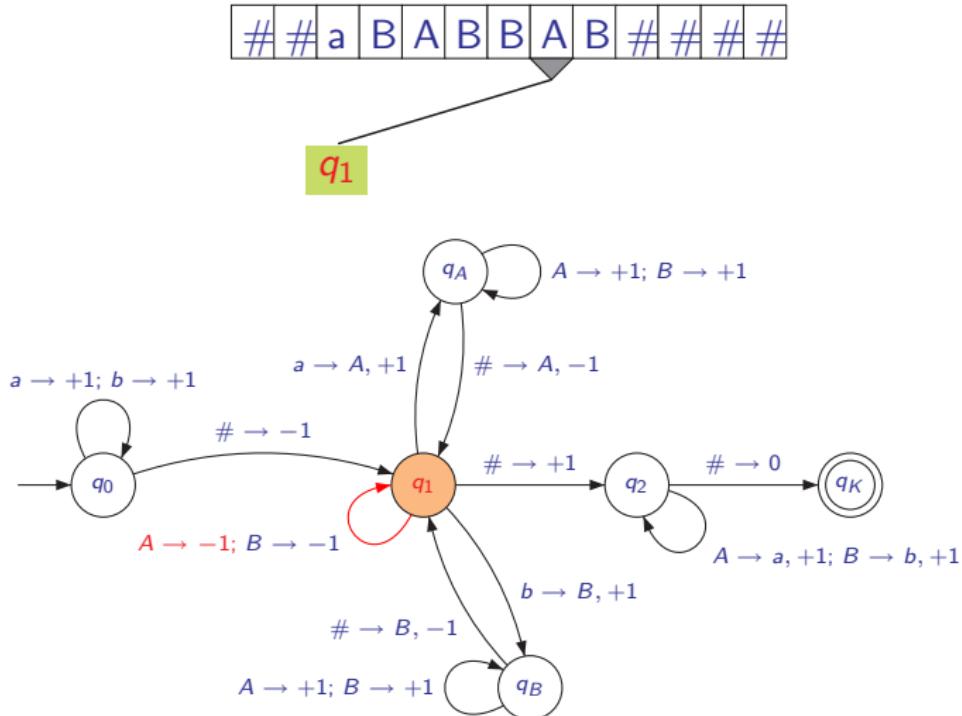
$$\delta(g_B, B) \equiv (g_B, B + 1)$$

$$\delta(q_B, \#) = (q_1, B=1)$$

$$\delta(g_2, A) = (g_2 - 3 + 1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, \#) = (q_1, \#, 0)$$



Popis

- TS hledá symboly **abab**, které následně označí.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

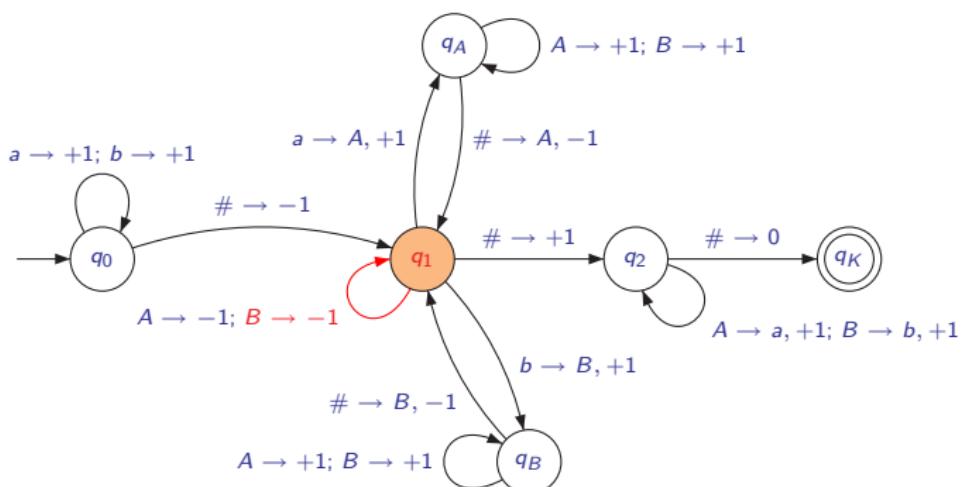
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá symboly abab, které následně označí.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

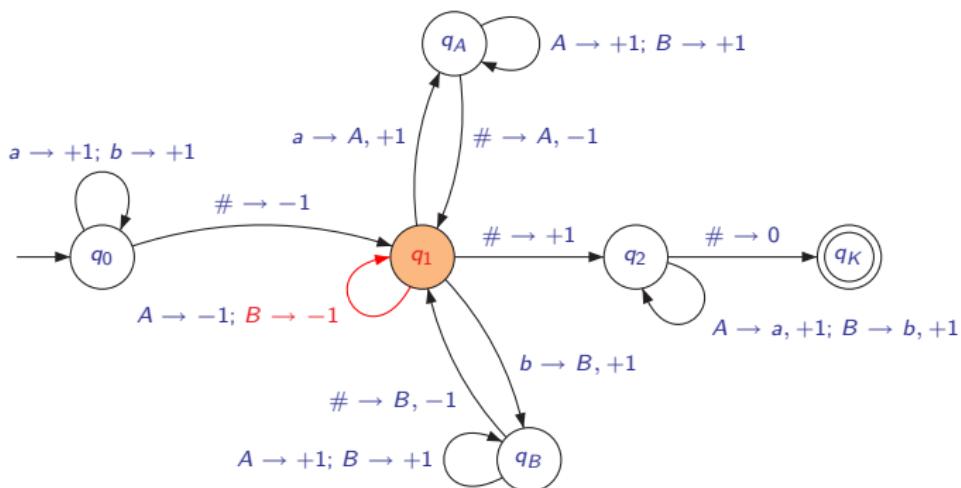
$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



$q_1$



## Popis

- TS hledá symboly **abab**, které následně označí.

## Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

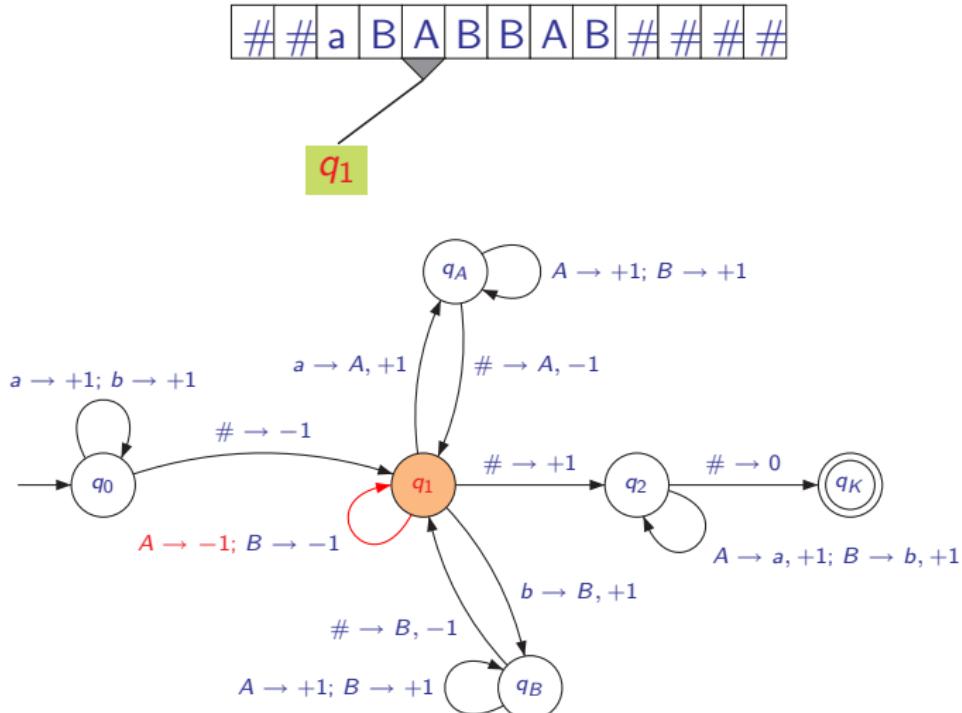
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(g_2, A) = (g_2, \beta + 1)$$

$$\delta(q_2, B) = (q_2, b + 1)$$

$$\delta(q_2 \#) = (q_K \# 0)$$



Popis

- TS hledá symboly **abab**, které následně označí.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

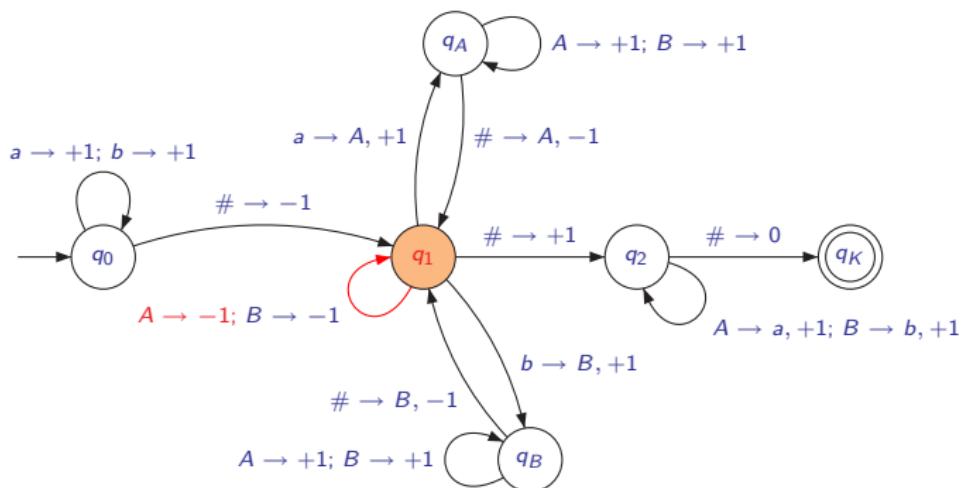
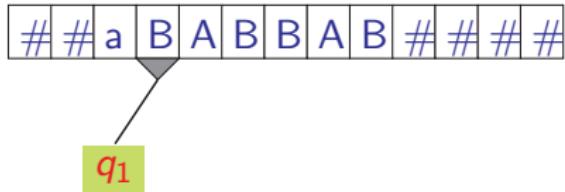
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá symboly **abab**, které následně označí.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

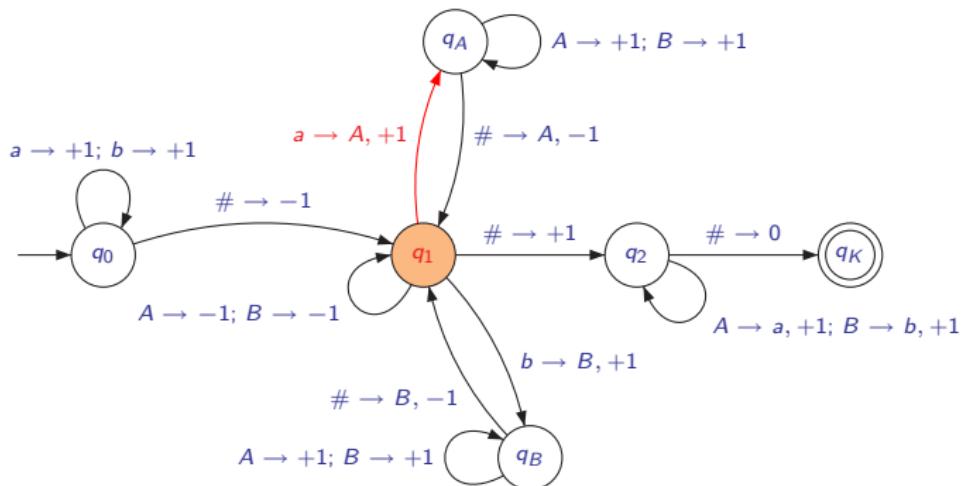
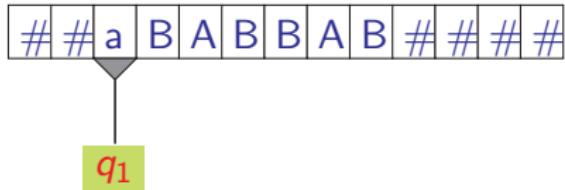
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá symboly abab, které následně označí.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

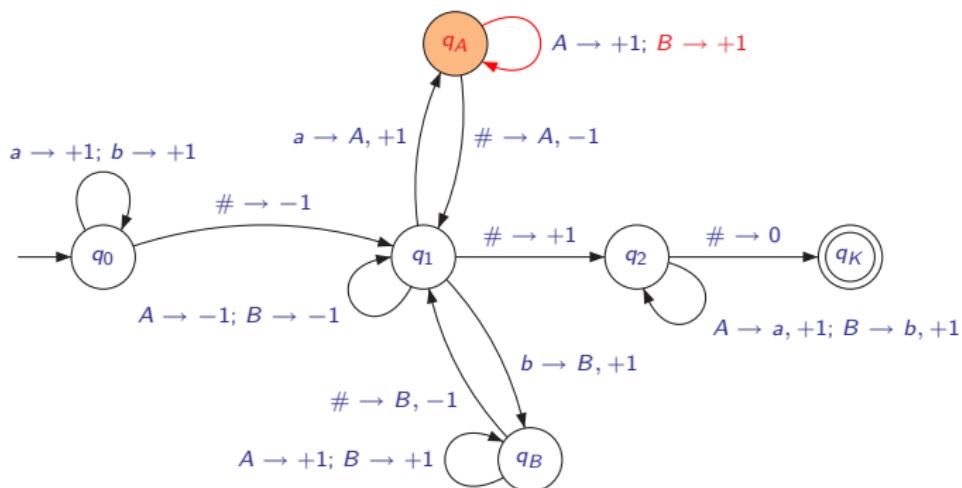
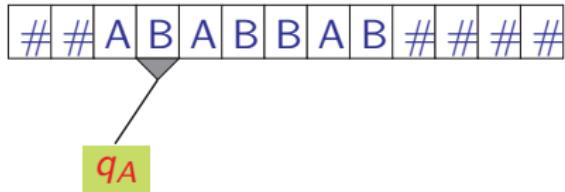
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá první volnou pozici, na kterou uloží symbol A.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

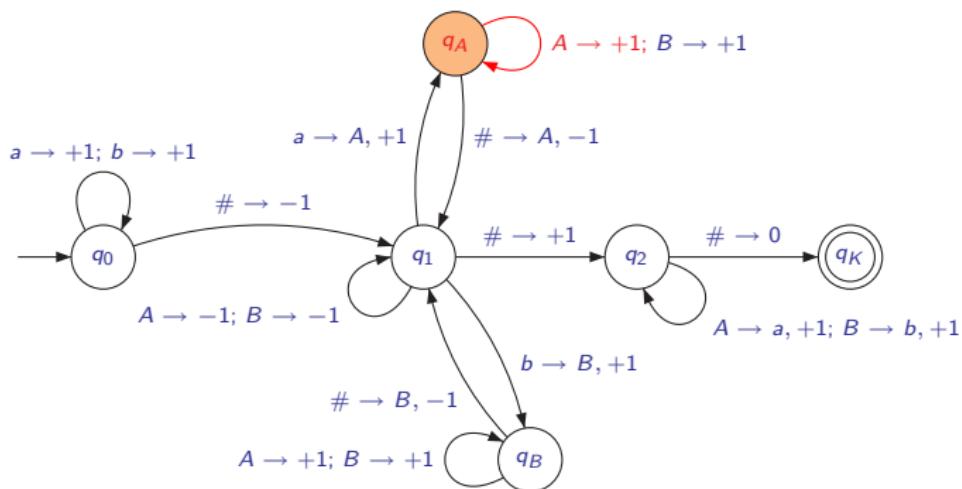
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá první volnou pozici, na kterou uloží symbol A.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

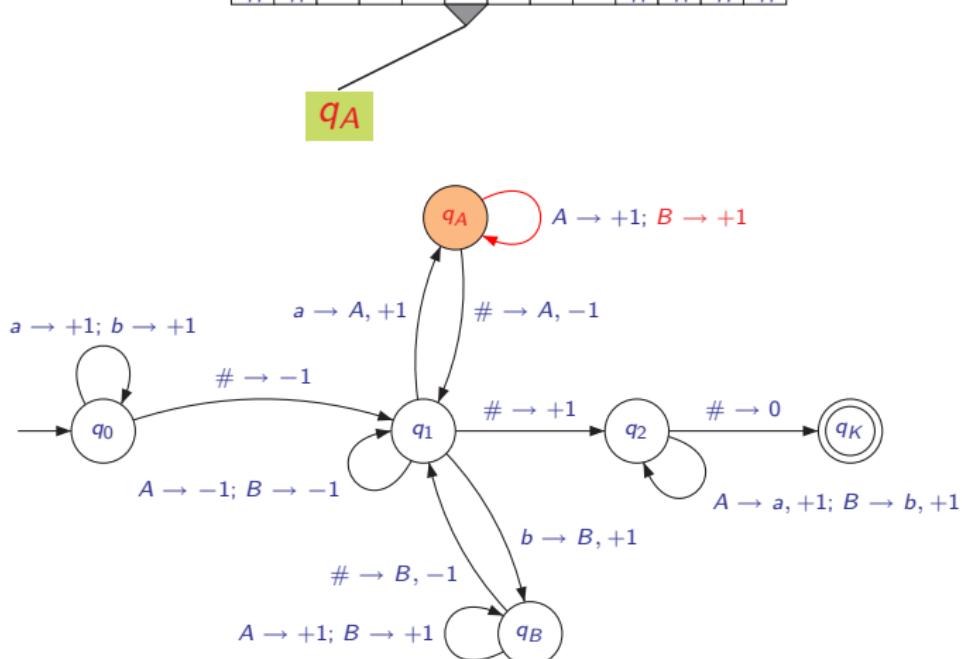
$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$

# # A B A B B A B # # # #



## Popis

- TS hledá první volnou pozici, na kterou uloží symbol A.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

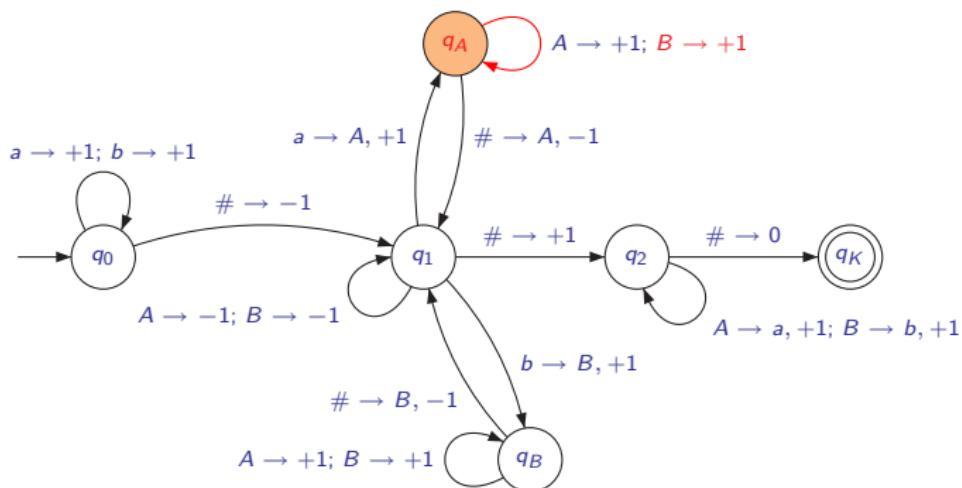
$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



$q_A$



## Popis

- TS hledá první volnou pozici, na kterou uloží symbol A.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

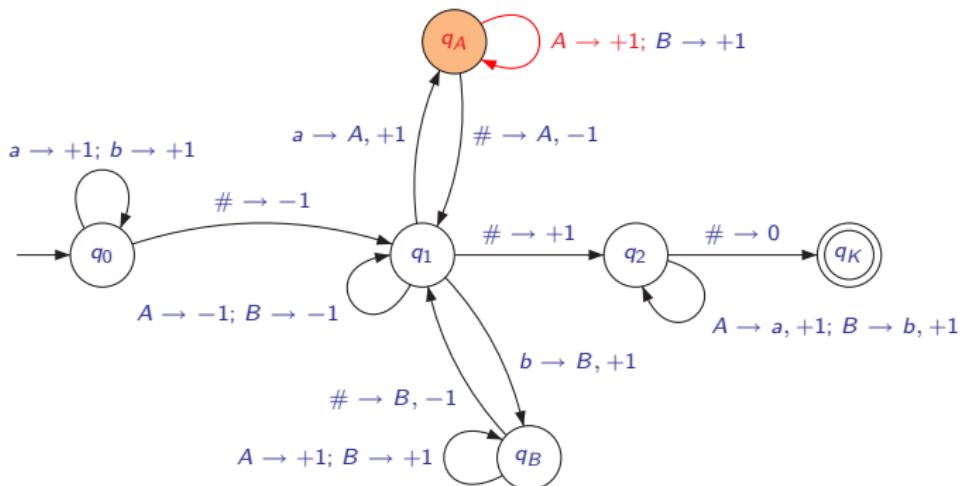
$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



$q_A$



## Popis

- TS hledá první volnou pozici, na kterou uloží symbol A.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

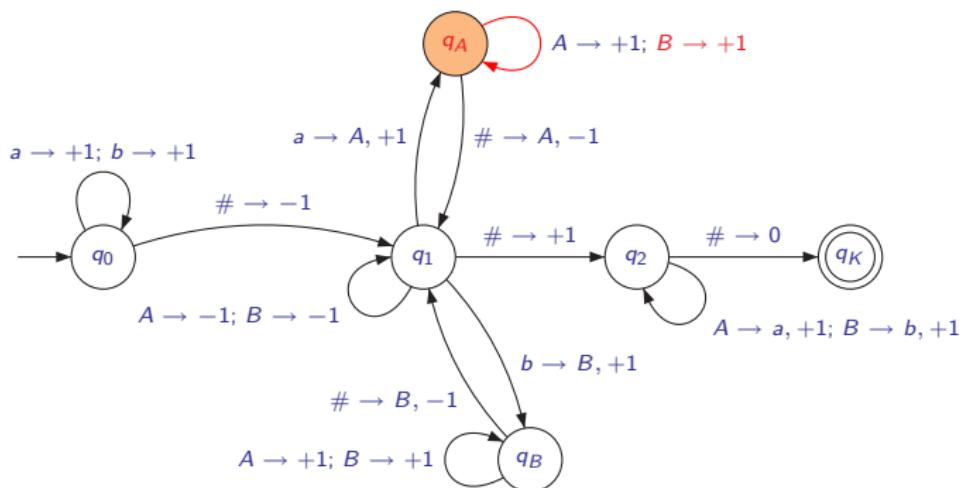
$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$

#	#	A	B	A	B	B	A	B	#	#	#	#
---	---	---	---	---	---	---	---	---	---	---	---	---

$q_A$



## Popis

- TS hledá první volnou pozici, na kterou uloží symbol A.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

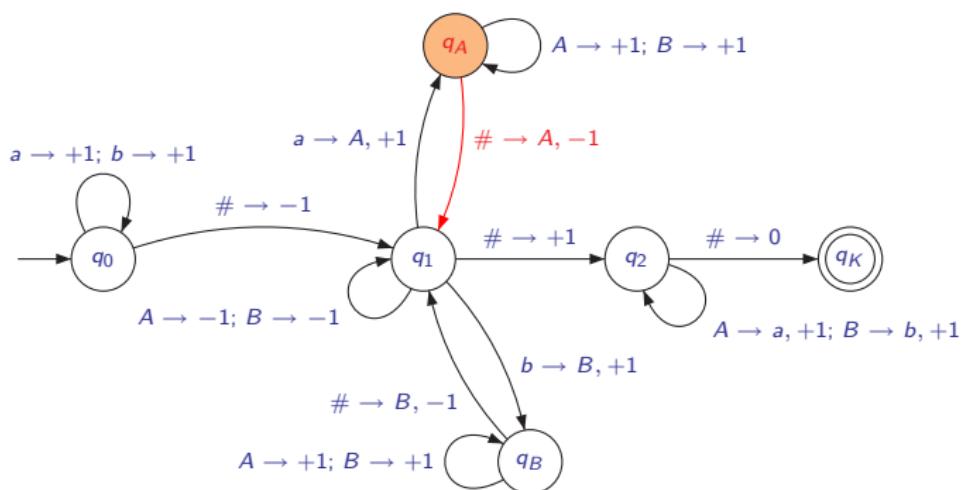
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá první volnou pozici, na kterou uloží symbol A.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

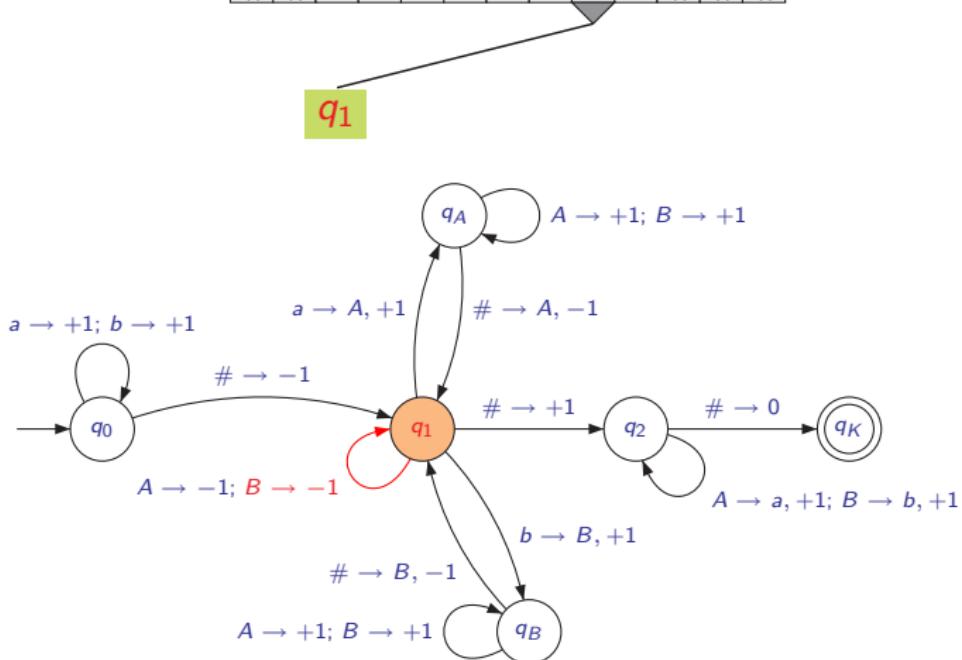
$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$

#	#	A	B	A	B	B	A	B	A	#	#	#
---	---	---	---	---	---	---	---	---	---	---	---	---



## Popis

- TS hledá začátek slova.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

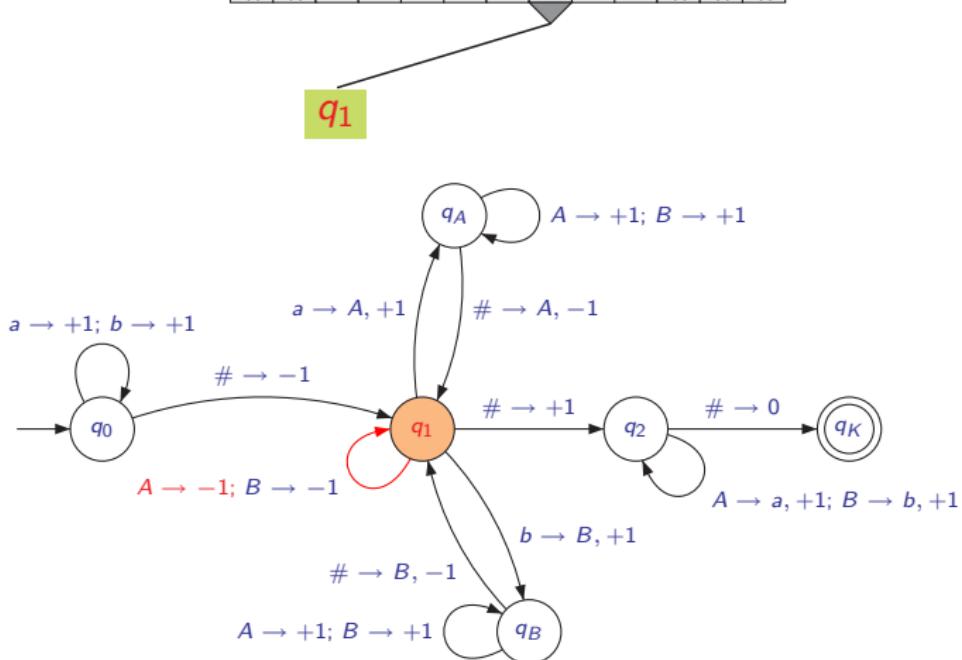
$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$

#	#	A	B	A	B	B	A	B	A	#	#	#
---	---	---	---	---	---	---	---	---	---	---	---	---



## Popis

- TS hledá začátek slova.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

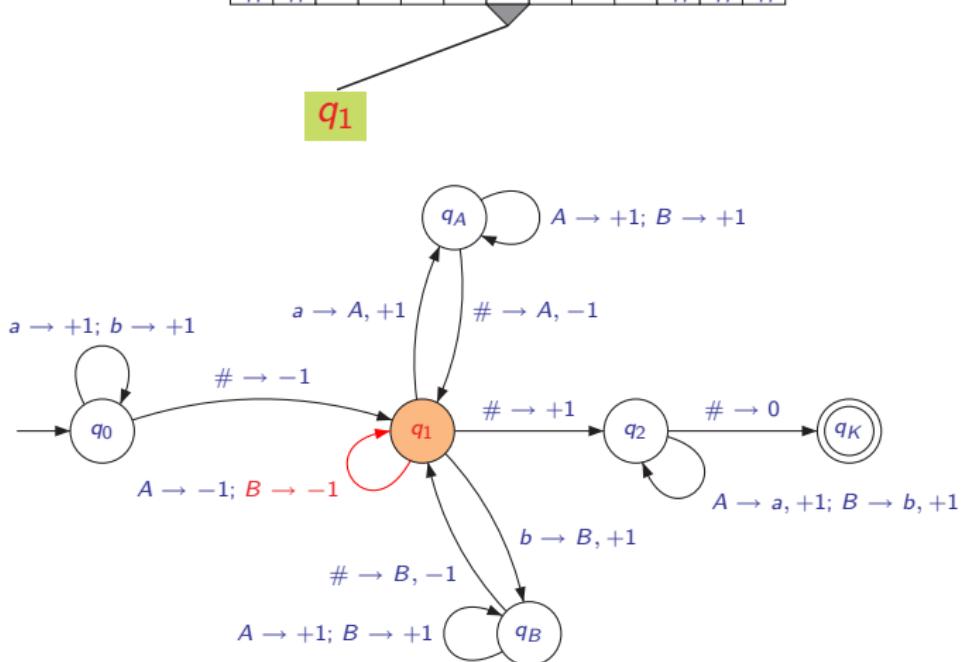
$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$

# # A B A B B A B A # # #



## Popis

- TS hledá začátek slova.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

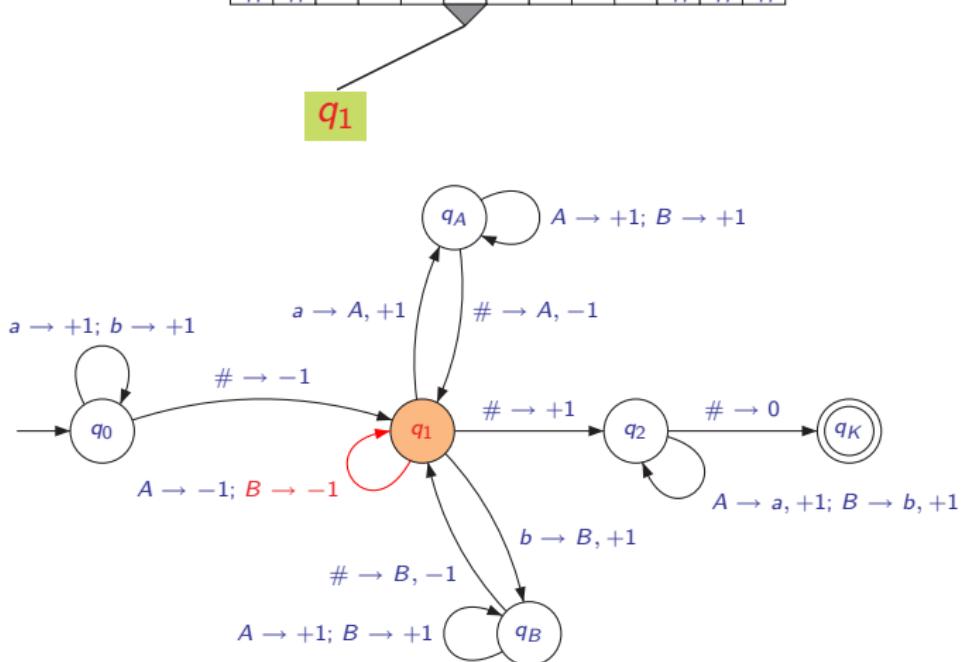
$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$

# # A B A B B A B A # # #



## Popis

- TS hledá začátek slova.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

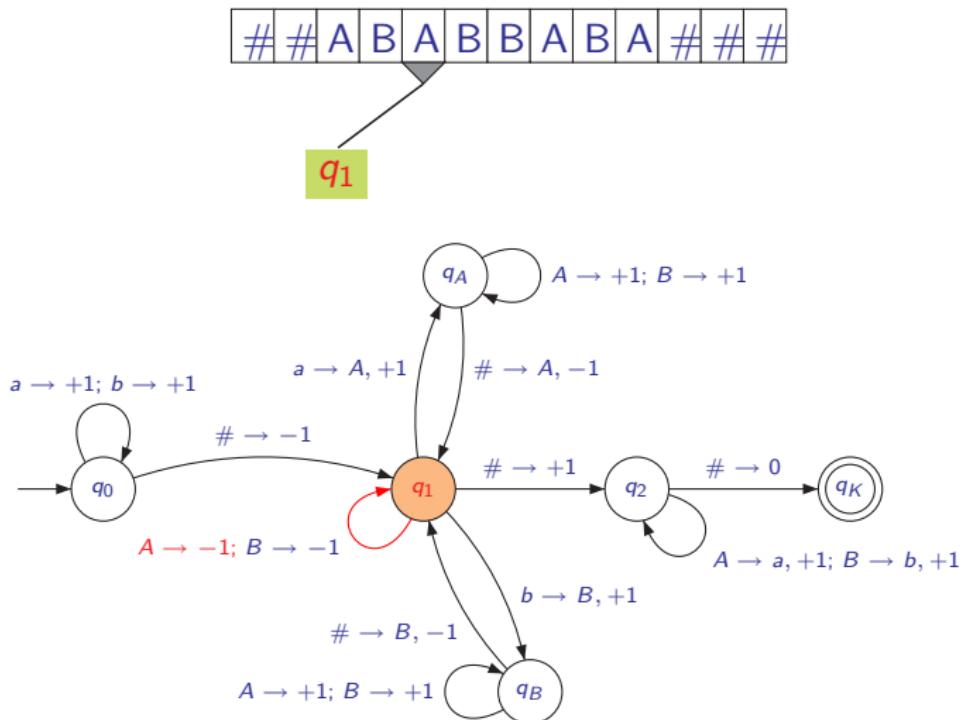
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá začátek slova.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

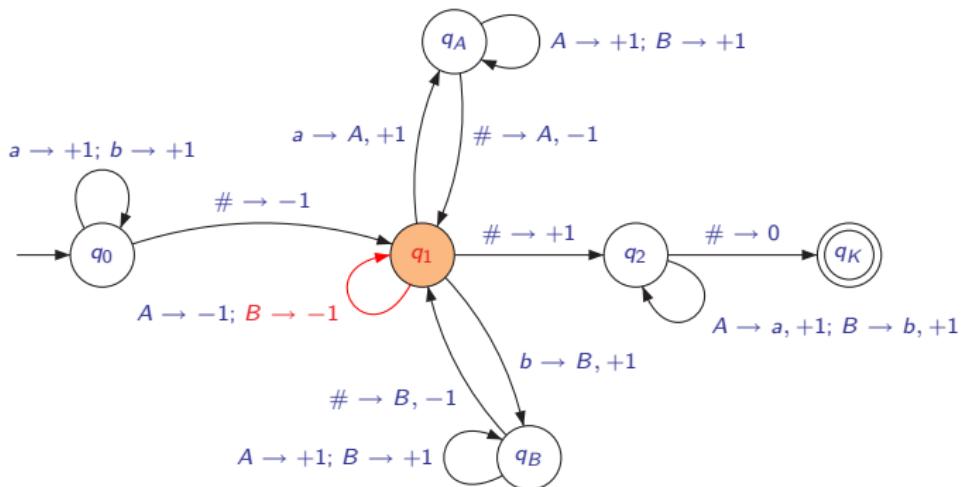
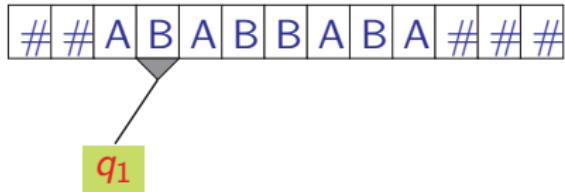
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá začátek slova.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

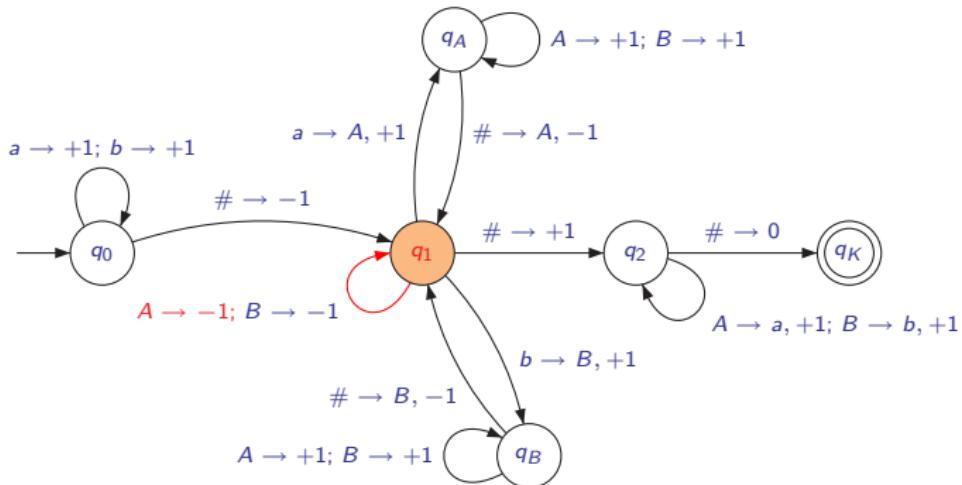
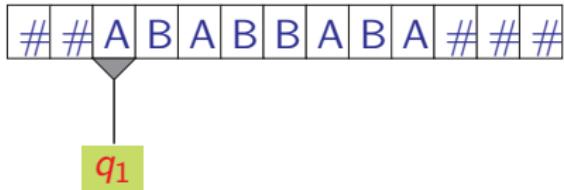
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá začátek slova.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

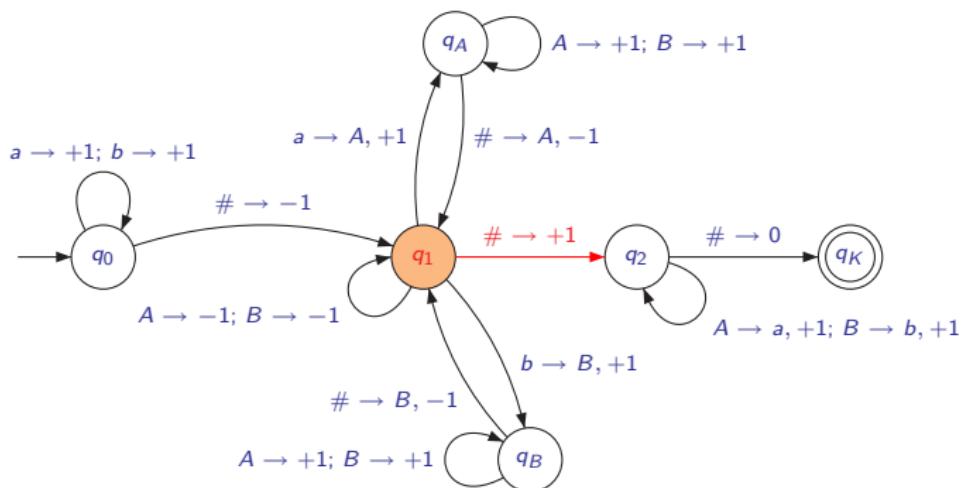
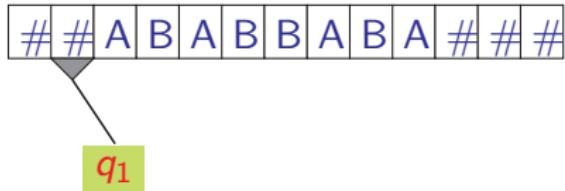
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS hledá začátek slova.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

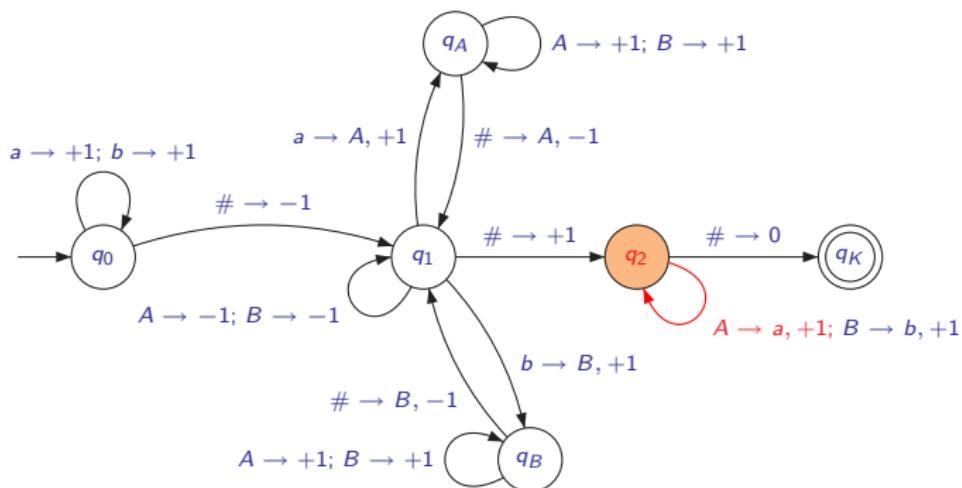
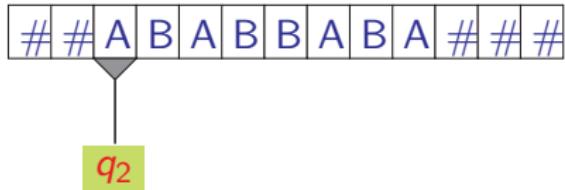
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- Nyní TS převede symboly 'A' na 'a' a symboly 'B' na 'b'.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

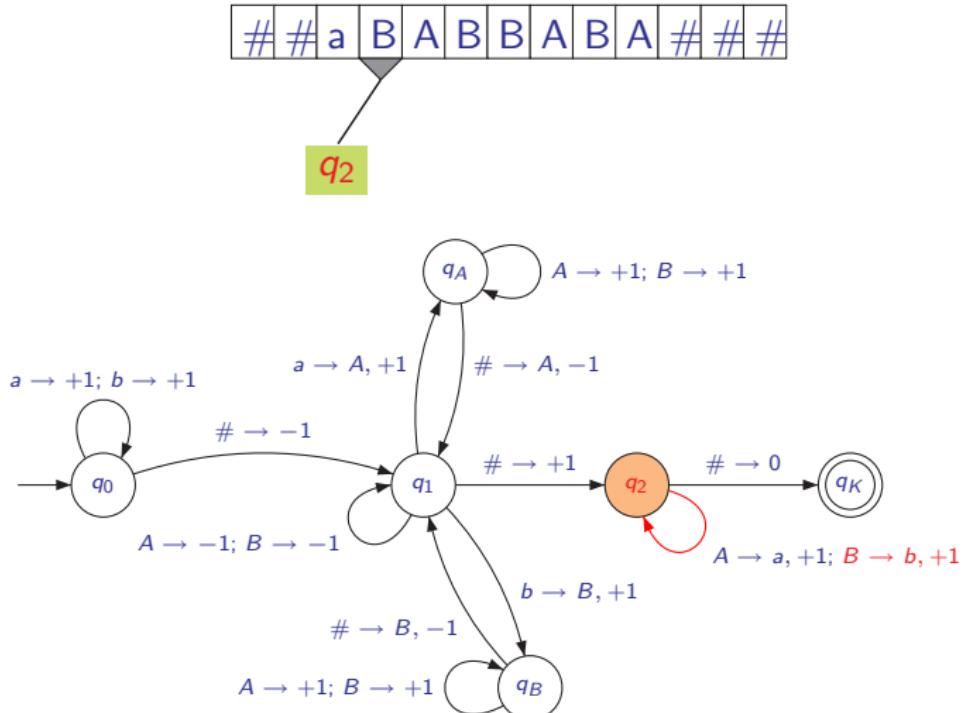
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- Nyní TS převede symboly 'A' na 'a' a symboly 'B' na 'b'.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

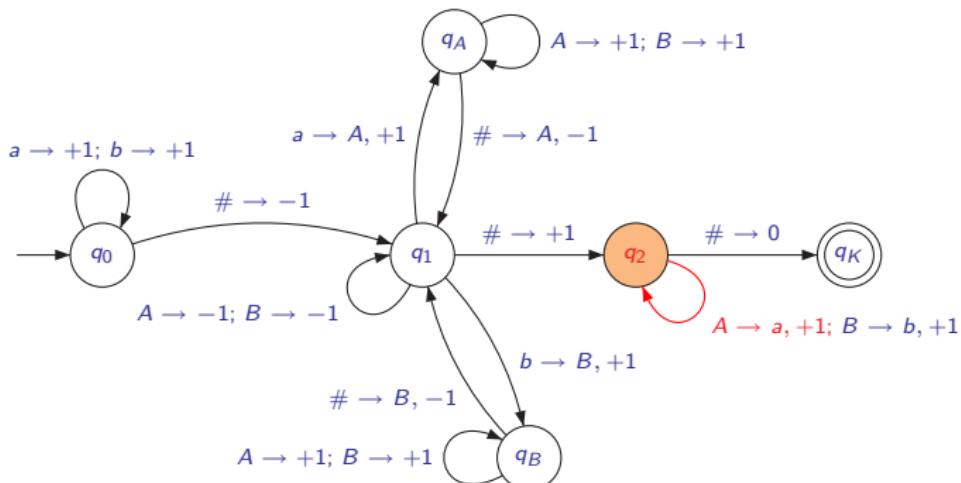
$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$

#	#	a	b	A	B	B	A	B	A	#	#	#
---	---	---	---	---	---	---	---	---	---	---	---	---

$q_2$



## Popis

- Nyní TS převede symboly 'A' na 'a' a symboly 'B' na 'b'.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

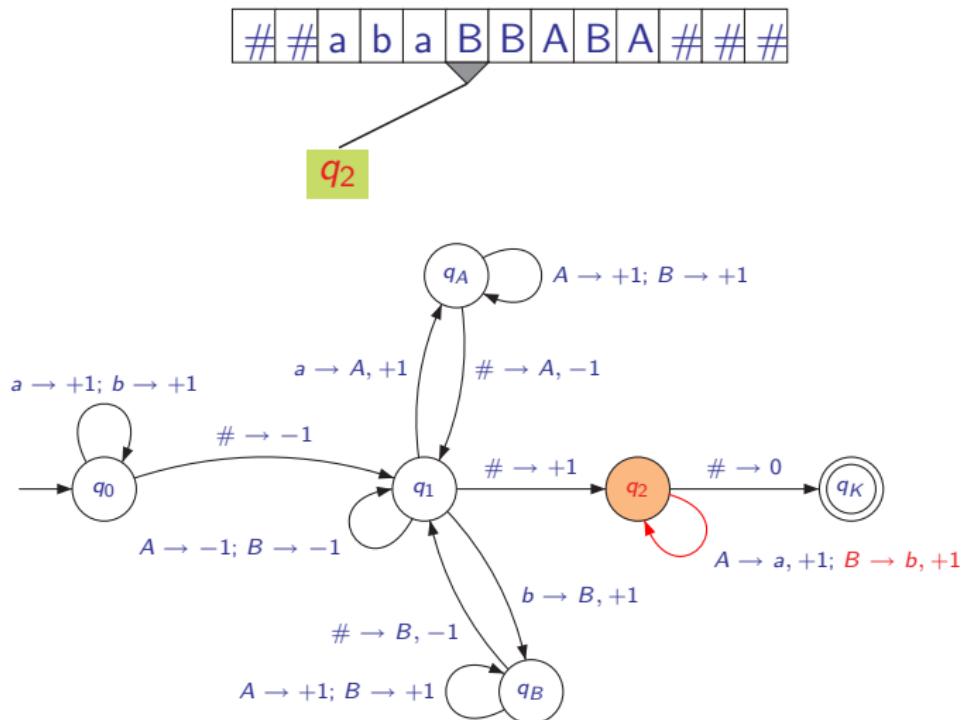
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- Nyní TS převede symboly 'A' na 'a' a symboly 'B' na 'b'.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

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$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

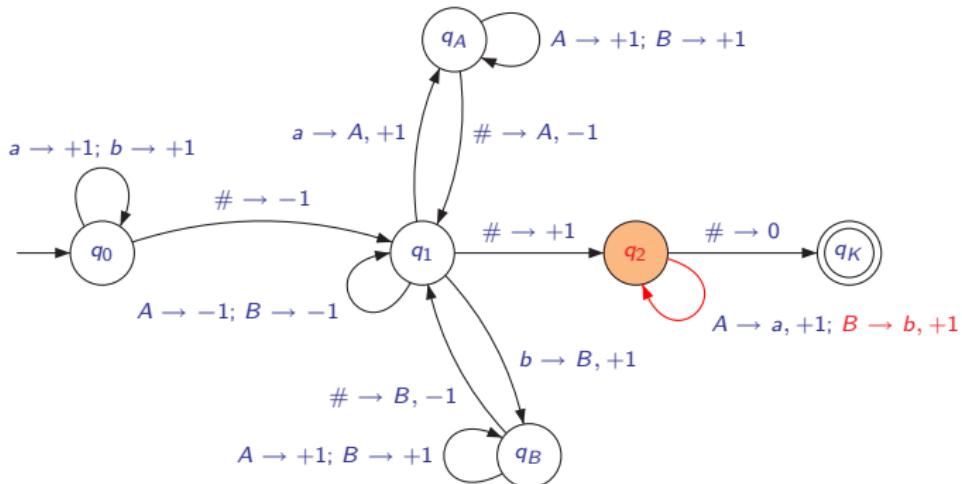
$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$

#	#	a	b	a	b	B	A	B	A	#	#	#
---	---	---	---	---	---	---	---	---	---	---	---	---

$q_2$



## Popis

- Nyní TS převede symboly 'A' na 'a' a symboly 'B' na 'b'.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

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$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

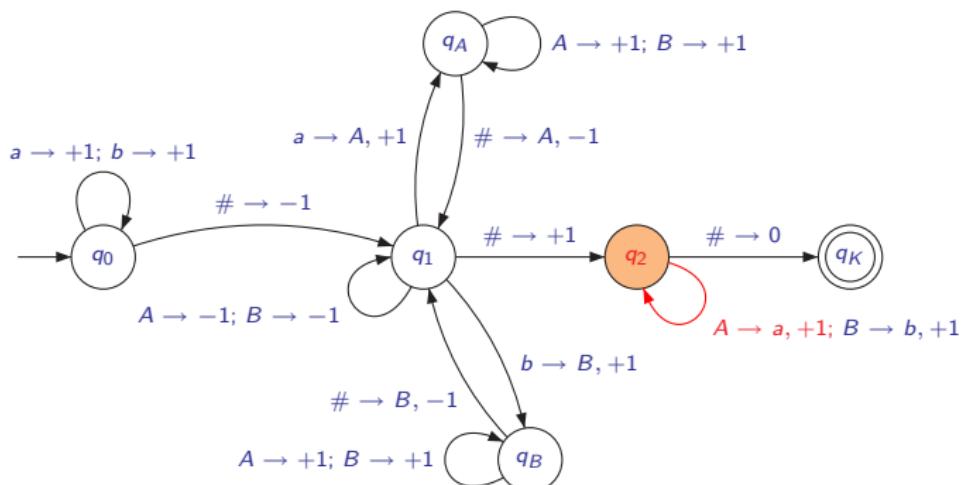
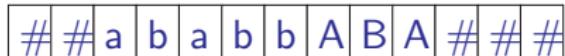
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- Nyní TS převede symboly 'A' na 'a' a symboly 'B' na 'b'.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

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$$\delta(q_1, A) = (q_1, A, -1)$$

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$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

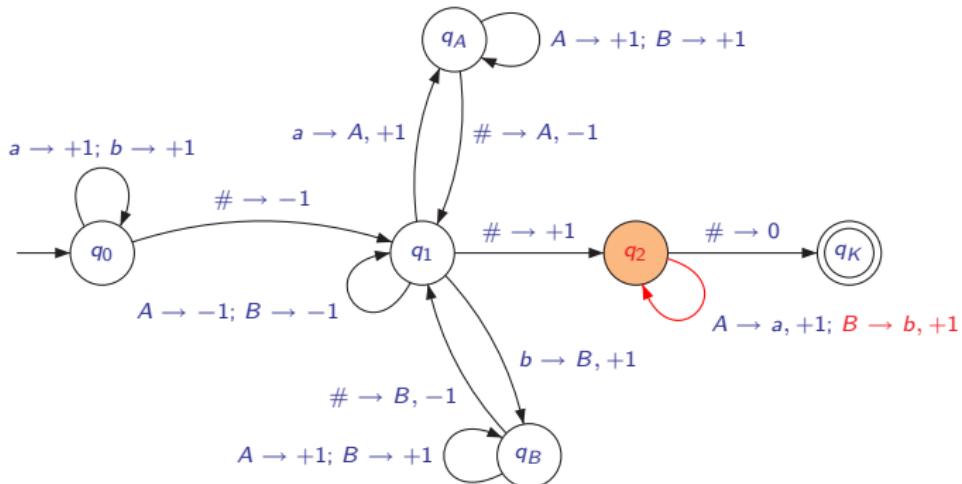
$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$

#	#	a	b	a	b	b	a	B	A	#	#	#
---	---	---	---	---	---	---	---	---	---	---	---	---

$q_2$



## Popis

- Nyní TS převede symboly 'A' na 'a' a symboly 'B' na 'b'.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

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$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

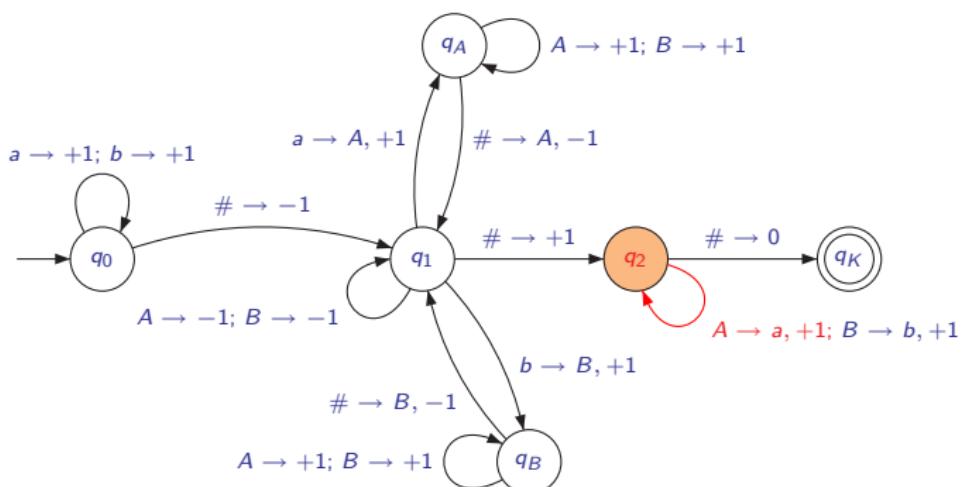
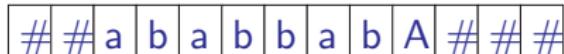
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- Nyní TS převede symboly 'A' na 'a' a symboly 'B' na 'b'.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

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$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

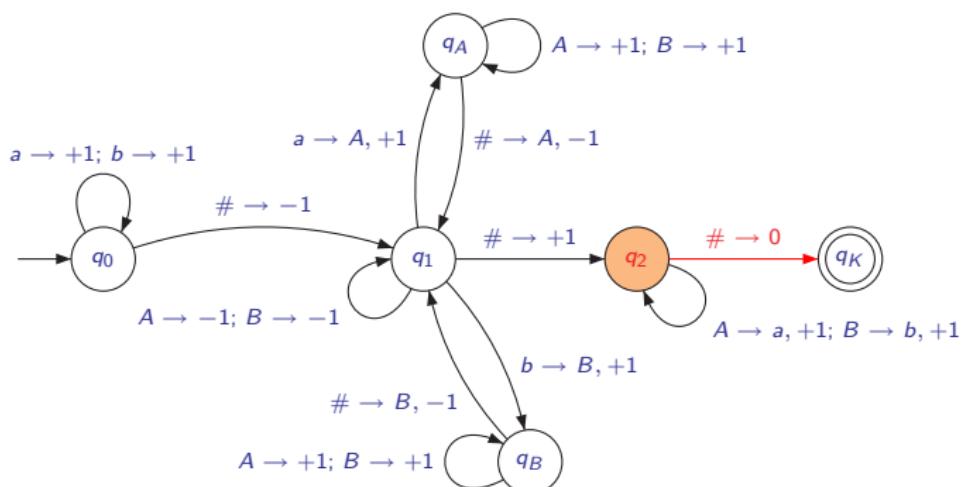
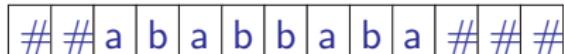
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- Nyní je na páscce zrcadlový obraz slova.

# Turingův stroj

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

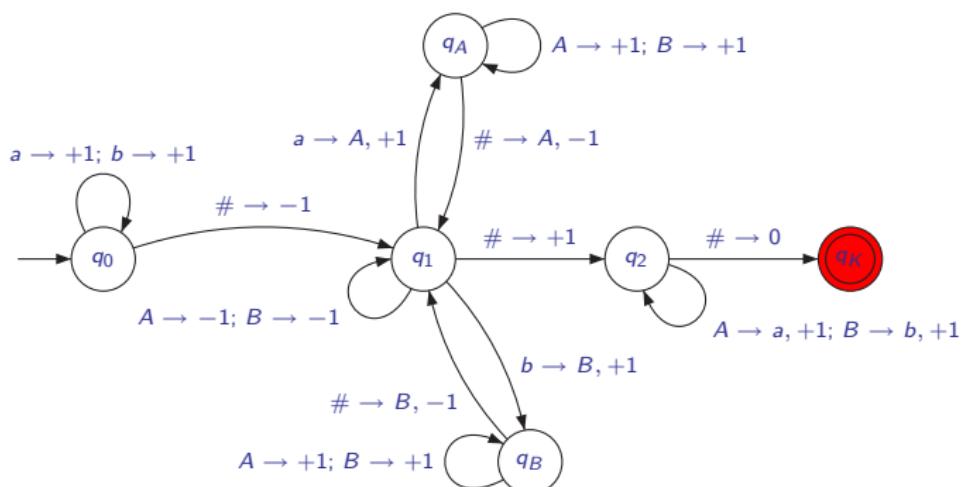
$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$



## Popis

- TS je v koncovém stavu.

## Popište činnost TS

## Popište činnost TS

Daný TS vytvořil ze vstupního slova  $w=abab$  výstupní slovo  $w=ababbaba$ .

Daný TS tedy tvoří zrcadlový obraz slova ( $w(w^R)$ ).

## Shrnutí

Turingův stroj vytvořil v průběhu výpočtu zrcadlový obraz slova na pásce.

vstup: slovo  $w = abab$

výstup: slovo  $w(w)^R = ababbaba$

Turingův stroj je určen šesticí parametrů  $M = (Q, \Sigma, \Gamma, q_0, F, \delta)$

- stavy:  $Q = \{q_0, q_1, q_2, q_A, q_B, q_K\}$
- vstupní abeceda:  $\Sigma = \{a, b\}$
- páskové symboly:  $\Gamma = \{a, b, A, B, \#\}$
- počáteční stav:  $q_0$
- množina koncových stavů:  $F = \{q_k\}$
- přechodová funkce:  $\delta$  viz další slide

## Přechodová funkce

$$\delta(q_0, a) = (q_0, a, +1)$$

$$\delta(q_0, b) = (q_0, b, +1)$$

$$\delta(q_0, \#) = (q_1, \#, -1)$$

$$\delta(q_1, a) = (q_A, A, +1)$$

$$\delta(q_1, b) = (q_B, B, +1)$$

$$\delta(q_1, \#) = (q_2, \#, +1)$$

$$\delta(q_1, A) = (q_1, A, -1)$$

$$\delta(q_1, B) = (q_1, B, -1)$$

$$\delta(q_A, A) = (q_A, A, +1)$$

$$\delta(q_A, B) = (q_A, B, +1)$$

$$\delta(q_A, \#) = (q_1, A, -1)$$

$$\delta(q_B, A) = (q_B, A, +1)$$

$$\delta(q_B, B) = (q_B, B, +1)$$

$$\delta(q_B, \#) = (q_1, B, -1)$$

$$\delta(q_2, A) = (q_2, a, +1)$$

$$\delta(q_2, B) = (q_2, b, +1)$$

$$\delta(q_2, \#) = (q_K, \#, 0)$$